

PEOPLE'S DEMOCRATIC REPUBLIC OF ALGERIA
MINISTRY OF HIGHER EDUCATION AND SCIENTIFIC RE
OF SCIENTIFIC RESEARCH
MOHAMED EL BACHIR EL IBRAHIMI UNIVERSITY
Faculty of Mathematics & Computer Science



MASTER THESIS

Presented for the graduation of *MASTER*

In : *Mathematics*

Speciality : *Operations research*

Through : *BOUKERROUI Sara*

Optimization of production, storage and distribution among factories,
warehouses and sales outlets.

Publicly defended, on ... / 09/2021, in front of the jury composed of:

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Promotion 2020/2021

Dedications

*To the cloud of my heart, to whom were the beginning and the end of
My reference and My way to you, My sister, My friend, My happiness
I swear to whoever planted your love in my heart that no one loves you like I
love you
to my heavenly star Heaven's gift "MAAFI Rahma"*

*Whoever drinks an empty cup to give me a drop of love ,To you my love mother
"TÉCHÉRAHINE Zoulikha"*

*For those who harvested thorns on my way to pave the way for knowledge, My hero
father "BOUKERROU Arezki"*

*To my friends, in memory of our laughter and good moments, in memory of everything
we lived...*

I hope with all my heart that our friendship will last forever.

*To my dear brothers, my dear sisters, my source of perseverance, courage and
generosity, my life will never be*

not so great without you. You are the best brothers, sisters in the world.

BOUKERROU Sara.

Thanks

Above all, I thank God Almighty for having paved the way for me throughout my lives, and for giving me the courage, strength and will to succeed. God is among me. He made it possible to complete this work and reach the present day, which is for me the starting point of a great adventure, the adventure of research and development.

To my teacher and supervisor, Dr. Maache Salah, I thank you for your presence, your sense of understanding and your hard work, which enabled me throughout these months to work in an atmosphere of trust and safety. Thank you for your invaluable help, for your wise advice and for the time you have devoted to me.

To the members of the jury, I thank you for the honor you bestowed upon me by accepting to sit on the jury of my brief. I am very pleased to be able to benefit from your contribution to improve the quality of my work. You will find in this work a testament to my sincere gratitude, appreciation and great appreciation.

Without forgetting to thank all the teachers who followed me during my university course.

Finally, I express my sincere gratitude to all the people who directly or indirectly contributed to the realization of this work.

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General introduction:

The business world is at the center of news and public debate. However, we often have difficulty measuring it, or even identifying it.

A Company is “a legally independent economic unit whose principal function is to produce products or services for the market.”

In other words, there is a business in which individuals mobilize their skills and energy, pooling material resources and money together to provide a product or service to customers.

Business is the core of our life, so it is necessary to get to know it better.

Corporations permeate economic and social life and energize our daily lives. As consumers, we depend every step of the way on these organizations that feed us, clothe us, transport us, entertain us, keep us healthy, and provide us with the communications, equipment and energy we need. As employees or entrepreneurs, we find in the company one of our main areas of expression. We invest a lot of our time, energy and creativity in it. We develop our skills there and emphasize our character.

Companies are all around us and yet we know very little about them. While the differences between companies are huge (size, age, number of employees, jobs, etc.), they are all grouped together under the same name, and industrial property is the space for manufacturing and warehousing apart from industrial lands, cold storage, special economic zones, Free Trade Zone, CFS, etc

So we use operations research to make it better

Operations research has its underlying foundations during the finish of WWII world where the American armed force approached several mathematicians, market analysts and IT experts to decide ideal and safe spots to introduce workstations against surveillance.

Notwithstanding, OR is an intersection where science, financial matters and figuring. Or then again can be characterized as a choice help apparatus which comprises of applying numerical (specialized) techniques to genuine financial issues including human and material assets and crude materials. These issues influence different regions like industry (creation the executives, booking, Assignment, transport ...), finance (spending the board, venture decision and portfolio ...), military (technique, support, ...) and numerous different regions.

By and large, genuine issues are hard to tackle taking into account their intricacies and the size of their information, consequently the need to utilize IT devices. Given a genuine issue, the OR approach comprises in dependably demonstrating (interpreting) this issue from reality to a numerical model and afterward applying a strategy (technique) for its goal to give arrangements on which choices will be made.

Introduction:

The aim of this chapter is to recall the essential concepts in a general framework Factory, warehouse, sales outlets model, some classic inequalities in these words and the properties and tools that we are going to use.

We introduce the product definitions, Product types, Warehousing and some essential properties. We will then give Order-picking systems, Batching of orders. As we know Difference between Warehouse and Factory structure, Difference between Warehouse and Distribution Center and relation between them.

At the end we introduce the definition of optimization, application, different types of optimization.

1. Factory:

A manufacturing facility is a structure or set of buildings in which items are fabricated. Manufacturing plants range in size from little studios to structures that fill a whole city. Laborers and machines in industrial facilities change crude materials, and parts, into prepared-to-utilize items. Processing plants produce practically all items that individuals use aside from food. Nonetheless, there are numerous plants that cycle, get ready and bundle food items. Processing plants resort to the rule of division of work, that is, they partition the necessary work into various separate activities. There are three types of factories:

- moduler factories
- errant factories
- Miscellaneous commodity factories

2.Product:

It is a general term that includes everything that is manufactured or prepared for the purpose of sale Marketing and export For individuals, groups or countries, including industrial, agricultural and service products. A commodity that the consumer can not Using it directly, as an office building or capital equipment, can be considered an indirect source of benefit as resale value or as a source of income. A commodity in the economy does not have to be morally or even legally acceptable. If a thing or service is sold at a positive price, it is a commodity because the buyer considers the utility of the thing or service more valuable than money. There are useful things, but they are not rare, like air For example, it is called a free good .

2.1. Product types:

2.1.1 Consumer Products:

They are the products that the consumer buys to use directly to satisfy his needs and desires, and he usually obtains them from retail stores. One of their specifications is that a large number of consumers buy them in small quantities every time or when they need them. The decision to buy them is affected by the personal payment of the consumer and their prices are usually much lower than the prices of production goods. There are three types of consumer goods are

- Affordable product: It is the consumer goods that the consumer buys without the need for much thought. It is easy in all stores. It is cheap and is always purchased from the nearest stores to the consumer, such as sugar, tea, soap, cigarettes, newspapers and magazines...etc.
- Shopping product: It is consumer goods that the consumer does not buy directly, but rather chooses between the alternatives offered in the market in terms of price, quality and brand. ..etc
- Special product: It is the consumer goods that the consumer makes an effort to obtain in order to distinguish them with special specifications or famous trademarks, and a large number of consumers do not accept to buy them from a few stores, and their sales are activated by advertising, such as watches, jewelry, sports equipment, and photocopiers.

2.1.2. Intermediate product (industrial):

They are the products that businesses or organizations use to produce other products or to manufacture the product after carrying out some production operations on them, and their advantages are the high cost of their purchase, the limited number of buyers, the participation of a large number of stakeholders in making the decision to purchase them after a thorough study. Examples include raw materials, semi-manufactured and manufactured parts, operating tasks, tools, machines and devices. Sometimes the leasing system for production goods, especially in electronic devices, may be followed due to the high prices or changing specifications constantly, or because their use is only seasonal. Marketing is one of the very important sciences for all economic activities, as it may lead to raising the sales of industrial activities to the sky or submerge the earth. Therefore, the salaries of marketing experts in major companies are very large.

2.2. product life cycle:

The product goes through several stages in its life, which are listed in order as follows:

- product development stage :
The process of product development is one of the main challenges in the field of marketing activity. Firms must think about finding new products for many reasons, including facing the decline stage of current products, facing intense competition, and reducing the risks of relying on one product.
- Submission stage:
This stage begins when the product is distributed for the first time to buyers in the market, and it usually takes some time to introduce the new product to the market, and this stage is characterized by a low rate of sales growth.
- growth stage :
It is the stage of increasing sales with rapid growth rates, as a result of the repurchase of the new product by the first consumers on the one hand, and the entry of a large number of traditional consumers to the market for this product on the other hand, which is a significant indication that the new products have entered the growing phase.
- maturity stage :

It is a stage during which sales numbers stabilize at a semi-constant level, except for a small increase at the beginning of this stage and a slight decrease at the end of it as well.

- decline stage :
Most of the products are on their way to decline, albeit over a different period of time and at different rates.

2.3 Clustering of related products:

In many stockrooms, certain items are regularly requested together. We will refer to such products as correlated products. We might lessen travel times for request picking by putting away connected items near one another in the distribution center (associated capacity). Clear instances of related items are: parts from similar provider or things of a similar shading or size. Corresponded items may likewise be distinguished from historical information. Frazelle and Sharp present a straightforward principle for distinguishing corresponded items from a provided request set. They play out a recreation investigation of a Miniload AS/RS where associated items are put away together in similar containers. They report decreases of 30-40% in the quantity of recovery trips.

Lee presents a grouping system for a request picking activity with man-on board S/R machines. The strategy initially makes bunches of associated items. Then, it gives a grouping of the bunches and the items in the bunches as indicated by expanding Cube-per-Order Index, COI (The COI is characterized as the capacity volume separated by the turnover pace of an item). In this way, it individually allocates the items to capacity areas following a space filling bend. At last, a trade routine endeavors to work on the arrangement. Appropriately, the strategy both considers request construction and recurrence.

The disintegration approach introduced by Lee appears to be encouraging, albeit the strategy for grouping the associated items looks self-assertive and extended. Rosenwein plans the issue of grouping connected items as a p-middle issue. The group middle is the item that has the most elevated relationship with different items in its bunch. The p-middle issue is the issue of discovering p groups with the most noteworthy relationship with the bunch medians. This issue might be tackled ideally with a branch-and-bound calculation.

The creators report that the calculation might take care of an ordinary issue inside 1 moment. Anyway the model definition, which incorporates the estimation of the relationship coefficients, is extended. A successful p-esteem is assessed from a movement distance estimation work. Van Oudheusden present a contextual investigation of a distribution center activity with man-on board S/R machines. Adjacent to a few different upgrades, they present corresponded stockpiling. They create groups of two corresponded items that are to be relegated to inverse stockpiling areas in the passageways so that these can be gotten to by the request picker in a solitary stop.

The issue of discovering a blending that limits the quantity of stops is polynomially resolvable as a Weighted Matching Problem. A recreation study dependent on genuine information shows a 46% decrease in movement time when allotting corresponded items to inverse stockpiling areas. Van Oudheusden and Zhu consider the issue of bunching corresponded items for an individual on board S/R machine in an activity with a set number of intermittent orders. These are orders containing the very lines that are mentioned consistently. They present a powerful programming heuristic that allocates the items in to capacity areas dependent on the repetitive orders. The calculation appears to be valuable in circumstances where there is little cross-over among the orders. In the event that the cross-over among orders expands, a bunching heuristic appears to be best.

2.4. Assignment of products to storage locations:

The Storage Location Assignment Problem (SLAP) concerns the task items to capacity areas. Such a task sets up a system for dispensing approaching burdens to capacity areas. Hausman et al. [3] present three stockpiling area task arrangements: randomized capacity, class-based capacity and committed stockpiling. The randomized stockpiling strategy permits items to be put away anyplace in the capacity region. The class-based capacity strategy disperses the items, in view of their interest rates, among various classes and for each class it holds a locale inside the capacity region.

Appropriately, an approaching burden is put away at a self-assertive open area inside its group. Under the devoted stockpiling strategy every area may just be utilized for a particular item.

Randomized and committed capacity are truth be told outrageous instances of the class-based capacity strategy: randomized capacity considers a solitary class and devoted stockpiling thinks about one class for every item. Class-based capacity and committed stockpiling endeavor to lessen the mean exchange times for request picking by putting away items with high turnover at areas that are effectively open. Randomized and class-based capacity are otherwise called shared capacity strategies, for these permit the progressive stockpiling of units of various items in a similar area.

3. Warehouse:

A warehouse is an arranged space for the capacity and treatment of product and material. (Fritz Institute) By and large, stockrooms are central focuses for item and data stream between causes of supply and recipients. Notwithstanding, in philanthropic stockpile chains, distribution centers differ enormously as far as their job and their qualities

3.1. Warehouse composed:

Stockrooms are regularly made out of a save stockpiling region just as a picking region, while a bed alludes to the unit of volume involving one stockpiling area. As open-case stock in the picking region is drained, new item is then moved from hold stockpiling to the picking region. The pickup and conveyance (P/D) point is the exchange point all through the storehouse.

3.2. Functions of a warehouse:

The two essential of functions a stockroom incorporate (1) transitory capacity and insurance of products and (2) offering some benefit added administrations, for example, satisfaction of individual client orders, bundling of merchandise, after deals administrations, fixes, testing, assessment and get together. To play out the above capacities, the stockroom is separated into a few useful regions, for example, hold stockpiling region, forward (request grouping) region and cross docking.

3.3. Types of Warehouse Space:

There are many types of warehouse space according to the factory and usage:

- Business: in leased structure utilized for business.
- Government or state, for example, at the ports or harbors. This is normal in crisis circumstances.
- Travel: for brief stockpiling of merchandise bound for various areas and need stockpiling for an exceptionally brief time frame.
- Fortified stockrooms: for capacity of merchandise whose obligation is neglected and particularly where the products are bound to another country. Pre-situated
- stock is regularly held in reinforced stockrooms so that fare is speedy and can some of the time be put away for significant stretches.
- Open stockpiling: not great for transient items but rather in crises, at times the lone other option.
- Space that is claimed and overseen by the association.
- Pre-created stockrooms where there are no long-lasting constructions accessible. This is normal practice in crises.

3.4. Warehousing:

Warehousing includes all development of merchandise inside stockrooms and Distribution Centers (Dc's), to be specific: getting, capacity, request picking, gathering, arranging, and transportation. A request records the SKU's and amounts mentioned by a client or by a creation unit, in a DC or a creation distribution center, individually. Request picking is the most common way of get-together SKU's that have been mentioned in a request at one time.

In a request picking activity. the request pickers might pick one request at that point (single request picking). A higher effectiveness might be accomplished by picking different orders at the same time (group picking). Besides, orders might be picked from isolated warehousing frameworks or separate zones inside frameworks. Therefore, in such circumstances the orders should be arranged and amassed to set up request honesty. Orders might be arranged during the request picking measure (sort-while-pick) or thereafter (pick-and-sort).

Warehousing frameworks might be characterized into three gatherings:

- (1) Picker-to-item frameworks.
- (2) Product-to-picker frameworks.
- (3) Picker-less frameworks.

In a picker-to-item framework, manual request pickers ride in vehicles along the pick positions. There is a wide assortment of vehicles accessible from physically moved vehicles to mechanized vehicles which additionally empower vertical development for request picking from raised positions. In-stead of a vehicle, a framework may likewise incorporate a remove transport for picked items (pick-to-belt).

Instances of item to-picker frameworks are the Auto-mated Storage/Retrieval System (AS/RS) and the merry go round. An AS/RS is a high-cove stockroom with Storage' Retrieval (S/R) machines or robotized stacker cranes that play out the capacity and recovery of capacity modules, (for example, buddy lets or holders). A minilad AS/RS is an AS/RS particularly prepared for the capacity and request picking of little things. A merry go round comprises of capacity places that pivot around a shut circle in this way conveying the mentioned SKU's to the request picker. Merry go rounds might turn skyline count (even merry go round) or in an upward direction (vertical merry go round).

Picker-less frameworks utilize robot-innovation or programmed gadgets. As for item recovery we recognize unit-load recovery frameworks and request picking frameworks. In a unit-load recovery framework complete unit-loads are recovered. In like manner, the vehicles either perform one stop (stockpiling or recovery) or two stops (stockpiling followed by a recovery) in a solitary outing. We allude to these outings as a solitary order cycle and a double order cycle, individually. In a request picking framework regularly not as much as unit-load amounts are picked, so that there will be various stops per trip (multi-order cycle).

3.4.1 Warehousing management:

We might set up excellent answers for warehouse administration by decaying the undertaking into various progressive sub issues. A clear-cut order will forestall neighborhood enhancement disregarding the worldwide setting. A wide order of the executives choices is the accompanying:

- Strategic choices.
- Tactical choices.
- Operational choices.

Key administration choices are long haul choices and concern the assurance of wide strategies and plans for utilizing the assets of an organization to best sup-port it is drawn out aggressive technique. Strategic administration choices basically address how to proficiently plan material and work inside the limitations of recently settled on essential

choices. Functional administration choices are restricted and present moment by correlation and act under the working requirements set out by the vital and strategic administration choices. The focal subjects of this overview are arranging and control of warehousing frameworks. Arranging of warehousing frameworks alludes to the arrangements, which are created at the strategic level concerning the task of merchandise to capacity areas. Control issues concern the genuine sequencing, booking and directing of the development of merchandise. Arranging and control choices are dependent upon vital administration and stock administration.

Vital administration characterizes long haul objectives and it comprises the production network association and the stockroom configuration Inventory the board chooses which items are kept away in what amounts and when shipments show up. Smart stock administration might decrease the stock levels and accordingly work on the effectiveness of the stockroom activity. Since these models both include the stock and the distribution center activity, the models build up a scaffold between the field of warehousing and the field of stock administration.

Since vital choices influence a significant stretch, these choices face high vulnerabilities. Commonplace techniques utilized for taking care of such issues are stochastic models and reproduction, in light of interest gauges. Arranging issues concern the middle of the road time frame and think about a current circumstance. Arranging calculations depend on chronicled information and endeavor to discover arrangements with a top notch normal exhibition.

Control calculations depend on real information and endeavor to discover arrangements with a top notch execution. Combinatorial enhancement strategies are appropriate for tackling arranging and control issues. Contextual analyses have shown that impressive usefulness upgrades are conceivable by applying shrewd arranging and control approaches.

4.Selling outlets:

Point of sale (POS) or point of purchase (POP) is the general setting at which retail deals happen. At the retail location, the dealer computes the sum due from the client, establishes that sum, can set up a receipt for the client (which can be a printed version check), and shows the client's installment choices. It is additionally where the client pays the shipper for merchandise or in the wake of giving him a specific assistance. After the installment has been gotten by the dealer, an exchange receipt can be given, which is frequently printed, yet can likewise be abstained from or sent electronically. To ascertain the sum due from a client, the trader can utilize different gadgets like scales, standardized identification scanners, and sales registers. To make an installment, installment gadgets, contact screens, and other equipment and programming are accessible. A retail location is regularly alluded to as an assistance point, since it is not just a retail location, yet additionally a state of audit or request for the client. The Software might incorporate provisions for extra usefulness, for example, stock administration, client relationship the board (CRM), monetary measurements, or warehousing.

Organizations are progressively accepting POS frameworks, and perhaps the most self-evident and convincing reason is that a POS framework takes out the requirement for sticker prices. Deal costs are connected to the item code when it is added to the store, the clerk essentially checks this code to finish the deal. In case there is a value change, this interaction should likewise be possible effectively through the customer facing facade. Different advantages incorporate the capacity to execute a few kinds of limits, a client dependability framework, and more productive stock control, and these elements are normal of practically all advanced electronic retail location frameworks.

4.1 Retail sales:

Retail trade , called retail selling, involves the sale of goods or merchandise from a specific place, such as a store , shop or kiosk , or by mail, in small or individual spaces for direct consumption by the buyer. Retail sales may include additional services such as delivery. Suppliers may be individuals or companies. In commerce, retailer or retail sales He buys goods or products in large quantities from producers or importers, either directly or through a wholesaler, and then sells small quantities to the end user. Retail establishments are often called boutiques or department stores. Retailers are at the end of the supply chain. Manufacturer marketers see segmentation as a necessary part of

overall distribution strategies. The term "retail" applies to services the needs of a large number of individuals, such as public utilities and electric power .

4.2. Order-picking systems :

In this segment we consider capacity area task all together picking frameworks. Jarvis and McDowell consider a request picking activity in an equal passageway stockroom where request pickers might get to the whole distribution center region. The creators make the presumption that a request picker navigates the whole path, after entering the walkway. In an ideal stockpiling task, the SKU's with the most elevated COI's top off one passageway, the SKU's with the following most elevated COI's go to the following walkway, etc.

In the event that the I/O station is situated toward the finish of the middle passageway, then, at that point the walkways nearest to the middle should convey the SKU's with the most elevated COI. This distribution is known as the organ pipe course of action. On the off chance that the I/O station is not situated symmetrically, an iterative method is utilized to dole out the walkways. The creators comment that the proposed stockpiling assignment engenders clog between request pickers. Guenov and Raeside consider class shapes for or-der-picking in one walkway utilizing a man-on board S/R machine. They think about an example with three class locales and visits with up to 30 picks. In all cases the class parcel seemed to influence the movement time.

The L-molded class segment could be improved by adjusting the class areas along the course of movement when the crane at the same time goes with greatest flat and vertical speed. A few creators have considered capacity area assignment in a square stacking climate. The principle issue for block stacking configuration is the assurance of the path profundities to limit extra room and additionally dealing with time. A few models have been introduced that permit a solitary path profundity all through the stockroom.

Goetschalckx and Ratliff present an effective unique programming calculation for limiting extra room that permits a predetermined number of pre-indicated path profundities. Their examinations show that it is attractive to have various different path profundities yet close to five. For additional re-search the creators notice that a few suppositions should be tried by and by and that lengthy methods ought to be fostered that fuse extra room and dealing with time contemplations. For a broad writing study on block stacking we allude to Goetschalckx and Ratliff. Roll and Rosenblatt examine the space requirements for assembled capacity versus randomized storage. It enjoys many benefits to store related items, e.g., items from the very shipment or items that are frequently mentioned together (associated items), near one another. A weakness might be the subsequent low space use. The creators play out a reproduction study to assess the expanded space prerequisites.

4.3. Batching of orders:

Clustering is a well known methodology for lessening the mean travel time per request. A cluster is a bunch of requests that is picked in a solitary visit. The orders in the bunch may not surpass the capacity limit of the request picking vehicle. Moreover, we might amplify the framework throughput by building up huge clumps with orders at adjacent pick areas. In any case, enormous clumps will bring about huge reaction times. In addition, just choosing orders at neighboring pick areas may unreasonably defer orders at the furthest finish of the stockroom. Appropriately, the compromise among proficiency and earnestness should be noticed. This compromise might be accomplished by choosing a square with the most critical orders (static methodology) and discover a request clumping inside the square that limits travel time. All orders in the square are executed before the following square is delivered.

Another methodology might be to dole out due dates to the orders and delivery each request quickly (dynamic approach). In this way, we set up a timetable that fulfills these due dates. Many bunching heuristics have been introduced in the writing for limiting travel time for the static approach. Most heuristics initially select a seed request for a group and accordingly extend the clump with orders that have nearness to the seed request as long as the vehicle limit isn't surpassed. The unmistakable factor is the action for the closeness of orders/groups. Armstrong .r consider bunching with fixed cluster sizes and present an Integer Programming model.

Elsayed , Elsayed and Stern , Gibson and Sharp and Rosenwein consider clumping in an equal path distribution center. Elsayed measures closeness by the quantity of normal areas. Elsayed and Stern consider varieties of this action and another action being the amount of the distances of every one of the areas in the up-and-comer request to the nearest area in the seed request. None of the actions appeared to deliver consistently predominant outcomes. Gibson and Sharp consider an action like the last measure in Elsayed and Stern and show that it outflanks a space filling bend approach.

Rosenwein utilizes two measures. One being the quantity of additional walkways that should be visited when a request is added to a cluster. Different midpoints the walkway numbers and clusters the orders for which this normal is closest. The previous measure outflanks the last in the analyses.

Elsayed and Unal, Gibson and Sharp, Hwang and Hwang and Lee consider request picking with man-on board S/R machines. Elsayed and Unal consider efficient heuristics. Gibson and Sharp utilize a space-filling bend. Hwang segment the rack into bunches of capacity areas and measure vicinity between orders by the crossover in the groups.

At last, Hwang and Lee consider for each request a locale in the rack that might be gone without expanding travel time. Vicinity is estimated by the crossover in these areas. Container and Liu suggest this heuristic in a comparative investigation of grouping heuristics introduced in the writing for man on board SIR machine activities. Few clumping strategies have been distributed that see due dates. Elsayed present a bunching heuristic that considers due dates for a request picking activity with man on board S,,R machines.

The goal is to limit earliness and lateness punishments. The heuristic initially sets up groups and accordingly determines the delivery times for the clusters. Elsayed and Lee consider sequencing and clumping of capacity and recovery orders to visits to such an extent that the complete lateness of the recovery orders is limited.

5.Difference between Warehouse and Factory structure:

Many use the terms warehouse and factory interchangeably. Some even say that “there is effectively no difference between a warehouse and a factory structure”. So, how different is a Warehouse different from a Factory structure?

We recall the definition of factory and warehouse each as mentioned earlier:

A warehouse is a commercial building generally used for storage of goods and warehousing is the process of proper storage and handling of goods and cargo using scientific methods in the warehouse and making them available easily and smoothly when needed. In recent days, warehousing is considered as one of the most important aspects of the trade.

A factory is an industrial site, usually consisting of buildings and machinery, or more commonly a complex having several buildings, where workers manufacture goods or operate machines processing one product into another and this is in demand in India currently due to the world looking for alternative supply chains to China (post-COVID-19) and proactive Central and State Governments who are promoting “Make in India”

Listed below the difference between a Warehouse and a Factory structure explained in detail:

Features	Warehouse	Factory
Location	Any where based on the demand	SIPCOT/ SIDCO (Government industrial parks) are most preferred
Power	3 phase is sufficient	High tension Power connection required to run heavy equipments and machinery
Floor height	4 feet above ground	Ground level
Flooring Capacity	5 metric ton / sqmt	10 - 15 metric ton / sqmt
Loading bays and canopy	Dock levelers needed with loading bays and canopy	Not required
Shutters	13 ft width – Normally 1 shutter per 5000 sft	above 18 ft (to allow movement of containers within the shed) – minimal number of shutters
Ceiling Height	To accommodate racking and vertical stacking	Height required for EoT and for temperature control
Type of building	RCC or PEB normally	Most commonly PEB (ACC for older structures)
EOT Crane (Electric overhead traveling)	Not required	Required to carry heavy load
Container access	Loading and Unloading of goods takes place outside the warehouse	Loading and Unloading of goods takes place within the factory itself
Employee Safety	Required, If Hazardous goods are stored, need to follow the safety procedures set by the Government	Occupational Safety, Health and Working Conditions of workers to be followed without deviation as per Government norms
Fire Safety	Required Depending on items stored – basic extinguishers and Hydrants are the norm of the day – Sprinklers depend on the material stored	Fire Hydrants with high storage water tank, Fire Extinguishers, Fire Sprinkler, Smoke Detectors and fire fighting drills at regular intervals are Mandatory requirements
ETP (Effluent Treatment Plant)/ STP (Sewage Treatment Plants)	Not required, as goods are only stored	Mandatory
Water source	Minimum quantity required	Required in large quantity
Pollution Control Certificate	Not Required	Depend on the types of goods produced

Table (1) : expresses the difference between a warehouse structure and a factory structure.

6. Difference between Warehouse and Distribution Center:

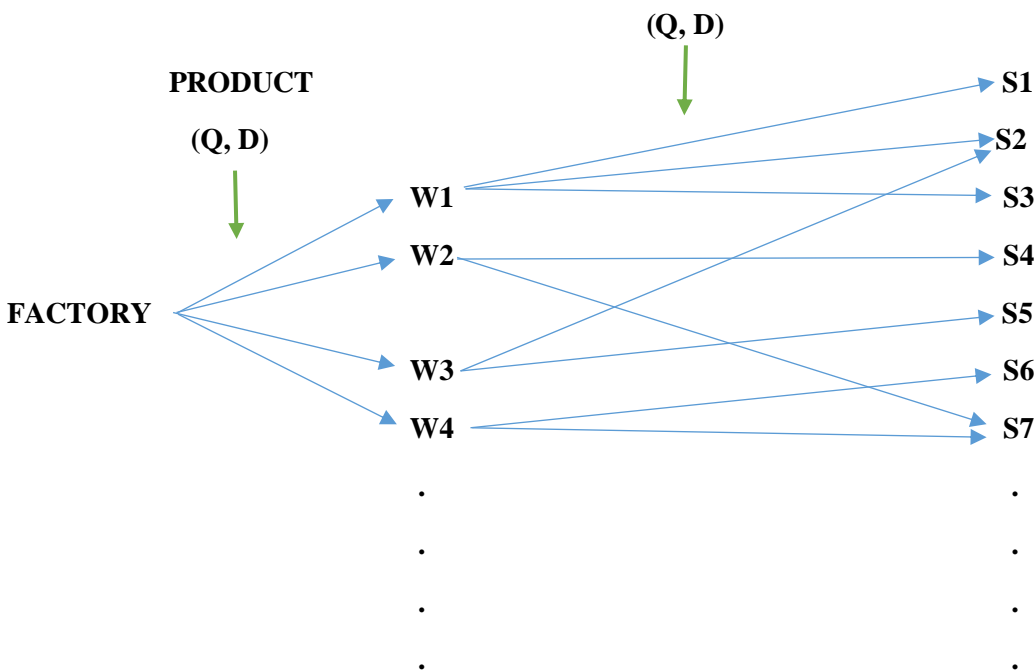
Some people are likely to mention warehouse and distribution center. However, not all of them understand the difference between warehouse and distribution center. The difference between the warehouse and distribution center is the system. In the old supply chain system, they usually prioritize regulations to increase the quantity of each product, anytime and anywhere. The regulation must be fulfilled because of the lack of information flow and planning mechanisms in the supply chain. Therefore, the warehouse was used for stockpiling supplies and the supplies would be sent out several months after arrived at the warehouse.

Nowadays, the supply chain has evolved and changed in the past hundred years. The modern supply chain is now equipped with better information and technology that can predict the demand for products or goods in the future, they can deliver goods on time. The new supply chain slogan is to be able to deliver the right goods, at the right place and at the right time. The traditional warehouse cannot fulfill the supply chain demand now and led to the evolution of traditional warehouses into distribution centers. Those are the simple understanding of the difference between the warehouse and distribution center. Commonly, the warehouse is used to store goods while distribution centers have additional services such as product mixing, order fulfillment, cross-docking, packaging, and others. Distribution center products usually have faster expiration periods compared to the warehouse. Basically, the flow velocity through the distribution center is faster than the flow rate through the warehouse.

Distribution center focused on the customer, this place becomes a bridge between the supplier and the customer. The main function of the warehouse is for storing goods efficiently, while the main function of the distribution center is to fulfill customer demands. Usually, orders from warehouses and retail are sent by distribution centers, not from the main warehouse. Then, the warehouse usually does not accept external customers, while the distribution center accepts orders from external customers. The mechanism at the distribution center is more complex compared to the warehouse in general. Therefore, the distribution center is equipped with the latest technology to manage the ordering process, warehouse management, transport management, and others.

Those are the difference between warehouse and distribution center and how distribution centers continue to grow over time. However, if you think that the warehouse is no longer needed now, you are totally wrong. The warehouse is still needed to handle some problems that will arise such as when in a month the demand for a type of product will increase and you need to stock the item in your warehouse.

Relation:



Schema expresses the relationship between the factories, the warehouses, sales outlets.

7. Optimization:

Optimization is a part of mathematics looking to show, examine and solve analytically or numerically the issues which comprise in minimizing or maximizing a function on a set.

Optimization assumes a significant part in operations research (a field at the boundary between software engineering, arithmetic and financial aspects), in applied math (principal for industry and designing), investigation and mathematical examination. , in insights for the assessment of the greatest probability of a conveyance, for the quest for methodologies inside the structure of game hypothesis, or even in charge and order hypothesis.

Numerous frameworks that can be depicted by a numerical model are enhanced. The nature of the outcomes and expectations relies upon the importance of the model, the ideal decision of the factors to be advanced, the effectiveness of the calculation and the means for computerized preparing.

- Optimization, in practice, we start with a concrete problem, model it and solve it mathematically (analytically: optimization problem, numerically: mathematical program).
- Minimum / maximum: let f be a function for which we want to find the maximum. The $\max_{x \in S} f(x)$ problem returns (x_0, v) while the $\min_{x \in S} f(x)$ problem returns $(x_0, -v)$. Thus, the search for a maximum can always be reduced to the search for a minimum.

7.1. Applications:

Optimization occurs in many areas:

- In operational research (transport problem, economy, stock managment...)
- In numerical analysis (approximation / resolution of system linear, non-linear ...)
- Automatically (system modeling, filtering, etc.)
- In engineering (dimensioning of structures, optimal design of systems (networks, computers, etc.))

7.2. Different types of optimization

7.2.1 Classification of optimization problems

➤ linear optimization

f is a linear function: $f(x) = \langle c, x \rangle$

S is defined by affine functions: $ax + b \geq 0$

- quadratic linear optimization

f is a quadratic convex function: $f(x) = \frac{1}{2} \langle Ax, x \rangle + \langle b, x \rangle$

A is a positive semi-defined symmetric matrix

S is defined by affine functions: $ax + b \geq 0$

- convex optimization

f is a convex function and S a convex domain

- differentiable optimization

f is a differentiable function

S is defined by differentiable functions (= constraints)

- non-differentiable optimization

ex: $f(x) = \max \{f_1(x), \dots, f_m(x)\}$.

- optimization in infinite dimension

ex: variation problems $J(x) = \int_0^T L(t, x(t), \dot{x}(t)) dt$ with x in a set of functions X , $x(0) = x_0$ and $x(T) = x_T$

➤ **Nonlinear optimization:**

There are three types of problem:

- Problem without constraints: $\min_{x \in \mathbb{R}^n} f(x)$.
- Problem with constraints of type equality: $\min_{x \in S} f(x)$ with S of the form $S = \{x \in \mathbb{R}^n \text{ t.q. } g_i(x) = 0 \text{ for } i = 1..l\}$ with $g_i: \mathbb{R}^n \rightarrow \mathbb{R}$.
- Problem with constraints of type inequality: $\min_{x \in S} f(x)$ with S of the form $S = \{x \in \mathbb{R}^n \text{ t.q. } h_i(x) \geq 0 \text{ for } i = 1..l\}$ with $h_i: \mathbb{R}^n \rightarrow \mathbb{R}$.

8.conclusion:

In the end we know the fundamental thoughts in the processing plant, stock, and outlets model of the mass framework and some normal awkward nature in these words, attributes, and gadgets we will utilize.

We likewise referenced the meanings of things, kinds of items, stockpiling and some essential attributes. Then, at that point, now, we gave the systems to choosing demands, and attracting demands. We comparably presented in warehousing structures and incorporate appropriation community the executives issues. We might have known about the contrast among stockroom and plant structure, the distinction among distribution center and dispersion focus and the connection between them.

Toward the end we have presented the significance of rearrangements, application and various sorts of optimization.

The objective of this chapter is to talk about warehouse model, mathematical model for warehouse and product, also planning and control of warehouse operations. While the first part Throughput capacity models Segments 2.1-2.3 spotlight on picking arrangements, grouping strategies, stockpiling task approaches, individually. Moreover, the assessment of option working situations through the advancement of movement time models will be talked about in Section 2.4.

Next in Storage capacity models Capacity scope organization models accept that request is either fixed or non-fixed. The main case is analyzed in Section 3.1, where we try to track down an exceptional stockroom size that fulfills some assistance prerequisite or limits costs. Segment 3.2 examines issues where request is non-fixed, in which case the ideal distribution center limit at various focuses in time not set in stone, that is, limit extension and constriction should be joined in the estimating choice. Techniques for augmenting space usage will be depicted in Section 3.3.

On other hands, we present a survey on methods and techniques for the planning and control of warehousing systems. Planning refers to management decisions that affect the intermediate term (one or multiple months), such as inventory management and storage location assignment. Control refers to the operational decisions that affect the short term (hours, day), such as routing, sequencing, scheduling and order batching. Prior to the literature survey, we give an introduction into warehousing systems and a classification of warehouse management problems.

1. Definitions:

Before proceeding with the discussion, we first define a number of terms. An order consists of a set of items belonging to one entity. The reorder quantity is the amount of stock of one item, which is received by the warehouse instantaneously.

A rack is a set of adjacent storage locations, and an aisle is the space in front of the rack where the order-picking vehicle travels. When discussing automated storage and retrieval systems (AS/RS's), it is customary to use storage/retrieval (S/R) machine or crane to denote an order-picking vehicle.

The term interleaving is also used to signify dual command, which consists of one leg from the P/D point to the first rack location where a pallet is placed, one leg from the first location to the second location where a pallet is retrieved, and a final leg back to the P/D point where the retrieved pallet is deposited.

The reserve area is where goods are held until they are required for shipment to the customer or for performing value added services or order collation. The latter is typically done in the forward area. The forward area could also be used to store fast movers that do not occupy much space.

2. Flow capacity models:

Sections 2.1-2.3 focus on picking policies, batching policies, storage assignment policies, and dynamic warehouse control, respectively. Additionally, the evaluation of alternative operating scenarios through the development of travel-time models will be discussed in Section 2.4.

2.1. Picking policies:

Goetschalckx (1983) states that the ideal coordinating under double order in a one-dimensional stockroom is accomplished by progressively blending the farthest unassigned stockpiling area with the farthest unassigned recovery area. He additionally shows that in a general multi-dimensional stockroom, the ideal double order picking strategy is gotten by tackling a task issue.

Graves, Hausman and Schwarz (1977) exhibit that, accepting an arbitrary stockpiling strategy and a first come - first served recovery line discipline, double order frameworks decrease expected full circle time by 32% as for single command. Except if in any case demonstrated, the rest of this segment accepts a multi-order two-dimensional

distribution center and a Chebyshev metric.

Bozer (1985) inferred a scientific articulation for the normal visit length of the band heuristic, just as the ideal number of groups. The band heuristic partitions the rack into various even groups, with picking performed following a serpentine way characterized by those groups. Hart, McGinnis, Shieh and White (1987) portray the closest neighbor sequencing heuristic, which includes joining every capacity area with the nearest accessible recovery area, in a double order climate. Since the rundown of recoveries changes through time, a 'block' of recoveries is chosen, the recoveries in the square are sequenced, and when the square of recoveries has been finished another square is selected. The expected throughput of the closest neighbor heuristic is demonstrated to be inside 8% of the upper bound on throughput execution for any square sequencing rule.

Kanet and Ramirez (1986) propose a blended zero-one non-straight programming detailing for the issue of choosing from substitute picking areas in order to limit a mix of breakdown cost just as fixed and variable picking costs. The variable expense is a component of movement time while the decent picking cost, disregarded in past investigations.

Cormier (1987) portrays a request picking issue in which the goal is to limit the absolute weighted lateness brought about when things are not conveyed to the P/D point before their particular due-dates. A powerful programming based heuristic is introduced where each work is a visit through the S/R machine, and each visit comprises of a few things each having distinctive due-dates however a typical consummation time. Request picking models depicted in this part don't expressly consider the speed increase and deceleration of the request picking vehicle. Guenov and Raeside (1989) give some experimental proof that the mistake accordingly instigated is insignificant.

2.2. Batching policies:

Bozer (1985) perceives the going with grouping alternatives: single-demand picking, pack picking, and zone picking. Under single-demand picking, everything of a solicitation are singled out a comparable trip, one solicitation for each excursion. Bunch picking believes a couple of requests to be grouped together on a comparable journey subject to as far as possible, but a solicitation ought to be done in a singular excursion. In zone picking, each vehicle works inside express geographical constraints of the dispersion community.

Pick-to pack structures are a kind of zone pickin. Bunch picking achieves venture assets over single solicitation picking whenever things on different orders can be taken care of meanwhile, especially when those things are arranged in closeness to one another in the stockroom. Regardless, bunch picking requires a solicitation blend stage which fuses total and sortation, with extended organization, equipment and district costs similar with single-demand picking. Additionally, certain applications require that orders apportioned to a comparative bunch be picked inside a comparative time window.

Following the game plan of bunches, a portable agent issue estimation is normally executed over each gathering to restrict hard and fast distance Utilizing reenactment showing, Barrett (1977) induced that without a doubt the main factor influencing the fundamental number of trips and the crane travel time is the amount of requests over which a particular solicitation gathering computation is executed. Packing not actually settled forever using gathering assessment by Hwang, Baek and Lee (1988), whose best estimation found the best plan in eight out of ten test issues.

Elsayed and Unal (1989) contemplated four solicitation amassing heuristics, under the doubts that indisputably the quantity of solicitations is customarily scattered, while the full scale number of things in a solicitation and the measure of everything are reliably spread self-assertive elements. Their best computation incorporates first . gathering each solicitation as immense or little with respect to in any case open to question some portion of vehicle limit. Then, at that point, tremendous orders are combined in pairs for which speculation assets over single-demand picking are figured. The pair achieving the greatest save reserves is kept and the association is reiterated until all colossal orders have been named to groups. Little orders are then seen as likewise, starting with the one having the greatest sum.

2.3. Storage assignment policies:

Hackman and Rosenblatt (1990) considered the allocation of items to an AS/RS when it has insufficient space to store all of them. The tradeoff to be optimized is between the cost of replenishing the items assigned to the AS/RS from their other warehouse locations, and the savings per retrieval request if an item is stored in the AS/RS. A heuristic algorithm is developed based on the relationship between this problem and the well-known knapsack problem. Once the allocation of items between the reserve and picking areas has been decided upon, as in the above, the items must then be assigned to storage locations. In a dedicated storage policy, a set of storage locations is reserved for each product for the duration of the planning horizon. Furthermore, since the same priority is given to all units of a product, these units are assigned to consecutive locations in the warehouse.

Goetschalckx and Ratliff (1990) demonstrate that shared storage policies, specifically those which assign storage locations on the basis of the duration-of-stay of individual units, yield significant reductions in rack size and travel time relative to dedicated storage systems.

2.3.1. Minimizing order picking costs:

Accepting racks of equivalent sizes, Hausman, Schwarz and Graves (1976) exhibited that turnover-based committed stockpiling decreases normal crane travel time by somewhere in the range of 26.3 and 70.6% concerning arbitrary capacity, contingent upon the interest dissemination. In class-based committed stockpiling, beds are appointed to a class of capacity areas dependent on their group of turnover, while inside some random class beds are put away haphazardly. Rosenblatt and Eynan (1989) report that a four-class (twelve-class) framework results in 90% (almost 100%) of the advantages of full turnover-based capacity task.

Utilizing recreation displaying, Linn and Wysk (1987) concluded that irregular stockpiling is best for low use, while turnover-based capacity is better at exceptionally high use. Request picking stockrooms are regularly described by countless little, quick things, with orders singled out multi-order visits. The ideal methodology is to find items with the most elevated likelihood of being remembered for orders on racks closest to the dock.

Sooner rather than later, it is attractive to fuse data about regular request profiles in the determination of capacity arrangements. Van Oudheusden, Tzen and Ko (1988), and Van Oudheusden and Weinan (1989) inspected a circumstance happening in a multi-order AS/RS rack, where orders are expected to repeat as per a known likelihood. The last determine an ideal arrangement dependent on unadulterated sequencing hypothesis for the instance of a one-dimensional rack and disjoint requests; heuristics dependent on this outcome are additionally portrayed for more broad issues.

2.3.2. Minimizing order picking costs plus inventory costs:

Wilson (1977) thought about the issue of setting up together a devoted stockpiling strategy and a stock arrangement. The calculation works by first setting all reorder amounts equivalent to the financial request amount (EOQ) and distributing stock by the COI rule. A slope search system is then used to produce another reorder amount vector, the COI rule is reapplied, etc, until the variety in reorder amounts between progressive cycles is tiny.

A comparative issue was additionally concentrated by Hodgson and Lowe (1982), then again, actually they utilized a persistent design portrayal of the capacity rack to manage huge issues in a modest quantity of PC time. They expand the block per-request file rule to the situation where travel costs per unit distance are not the equivalent for all things, that is, the movement autonomy condition doesn't hold.

Malmborg and Deutsch (1988) consider a climate where a blend of single-and dualcommand cycles is allowed, with stock expenses as accepted by Wilson (1977). Simple pursuit heuristics are proposed in which part estimates are successively decreased from their underlying EOQ levels, and stock areas relegated by the COI rule. Malmborg, Krishnakumar and Simons (1988) reason that this is the best technique since the arrangement quality is like that got utilizing inclination search and example search heuristics, while keeping away from the need to figure the slope of the expense work.

2.4. Performance evaluation models:

Travel-time models can be valuable in looking at elective working situations and distribution center plans. A few papers referenced beforehand which utilize this methodology are Hausman et al. (1976).

Graves et al. (1977), Bozer (1985), and Han et al. (1987). The accompanying creators present different and logical travel-time articulations for first-cut assessments. The examination performed by Bozer and White (1984) incorporates a few P/D point areas and abide point procedures, where the last alludes to the area of the S/R machine when it becomes inactive subsequent to finishing a cycle.

Seidmann (1988) fostered a movement time model for the circumstance where the quantity of things to be picked is an irregular variable, while Elsayed and Unal (1989) got an articulation to gauge the movement time as an element of the quantity of areas to be visited and the actual arrangement of the stockroom. Articulations for upper and lower limits on movement time are likewise evolved. Hwang and Ko (1988) determined travel-time articulations for multi-walkway AS/Rs', expecting that the S/R machine is moved between nearby paths by a 'traverser'. They likewise examine the issue of apportioning the paths into various classes to limit the necessary number of S/R machines subject to the throughput imperative, each class having a committed S/R machine. Kim and Seidmann (1990) show that recently distributed models are exceptional instances of their own throughput rate articulations.

Barely any endeavors have been made to join the manual piece of request picking undertakings into time guidelines. Foley and Frazelle (1991) expect the time needed for the picker to recover things from holders to be either deterministic or dramatically dispersed. Their motivation is to decide the most extreme throughput at which a miniload AS/RS can

handle demands, in capacity of such boundaries as rack measurements, S/R machine speed, etc. They likewise infer shut structure articulations for the likelihood circulation capacity of double order travel time, the use of the picker, and the use of the S/R machine. In complex circumstances where logical models are illogical, reenactment models are useful in evaluating execution measures. Expecting a solitary walkway double order AS/RS, Azadivar (1986) developed a reproduction model to assess framework reaction under different strategies. A streamlining issue is settled which amplifies throughput while regarding upper limits on most extreme line length and normal holding up time, just as the adequate dangers with which the imperatives can be abused. Likewise, reenactment models can likewise be applied to assess capacity limit and can be incorporated in worldwide advancement systems for stockroom plan.

3. Storage capacity models:

Storage capacity planning models assume that demand is either stationary or non-stationary.

The first case is examined in Section 3.1, where we seek to find a unique warehouse size that satisfies some service requirement or minimizes costs. Section 3.2 discusses problems where demand is non-stationary, in which case the optimal warehouse capacity at different points in time must be determined, that is, capacity expansion and contraction must be incorporated in the sizing decision. Methods for maximizing space utilization will be described in Section 3.3.

3.1. Stationary demand:

Jucker, Carlson and Kropp (1982) consider a firm creating a solitary item or administration, and which is wanting to extend its ability by building a plant to supply a few locales, each to be served by a provincial stockroom. Local distribution centers are rented to such an extent that there are no decent expenses related with them.

The goal is to discover the plant and stockroom limits which boost anticipated benefit, subject to no stock outs because of lacking plant limit. An effective calculation is created dependent on Kuhn-Tucker conditions.

Roll and Rosenblatt (1983) utilized recreation to decide the impact of the capacity strategy, stockroom size, just as the likelihood circulations of shipment appearance times, stockpiling times and number of beds per shipment on the assistance level of a distribution center. The assistance level estimates the quantity of beds which should be put away in outsider offices because of deficient ability to oblige approaching shipments inside the stockroom. Stockroom limit in a stochastic climate was again contemplated utilizing recreation by Rosenblatt and Roll (1988).

An (s, Q) stock arrangement and an irregular stockpiling strategy were accepted, s being the reorder point and Q the reorder amount. By and large, the distribution center limit important to keep not really set in stone assistance level was observed to be straightforwardly relative to the reorder amount and the normal every day requests, and conversely corresponding to the quantity of things, reorder point and the changeability in day by day interest. A multiplicative relapse model demonstrates that the last two elements have just a minor impact.

Roll, Rosenblatt and Kadosh (1989) created scientific and recreation models for the normal holder subordinate expense. As amounts increment, so does the ideal holder size, and the more prominent turns into the stockroom limit expected to keep a necessary help level. Additionally, the help level turns out to be progressively delicate to the distribution center limit as the all out number of things put away increments. At last, the expense of presenting two or more holders is generally higher than the expense of presenting just one.

3.2. Non-stationary demand:

White and Francis (1971) examined the issue of deciding the ideal size of a distribution center over a limited arranging skyline. Expenses relate to distribution center development, item stockpiling, and deficient stockpiling limit. The case in which changes are permitted in the stockroom size during the arranging skyline is defined as an organization stream issue for proficient arrangement. The issue of a firm wishing to limit the expense of renting distribution center space over a limited arranging skyline was concentrated by Lowe, Francis and Reinhardt (1979). An essential agreement for distribution center space is haggled preceding the start of the arranging skyline, for each time span. Interest for space

is thought to be an irregular variable with realized thickness work in every period. Quickly before the start of each time-frame, an auxiliary agreement is haggled to get adequate additional capacity accepting a known acknowledgment of the irregular variable. An avaricious calculation is portrayed for tackling the relating network stream plan. As shown in Cormier and Gunn (1991b), the annualized cost of giving peripheral extra room is overwhelmed by the common expense of the stock strategy. This implies that it is alluring to incorporate stock expenses in the issue to improve capacity limit. This class of issue was inspected by Levy (1974), accepting both deterministic and stochastic interest.

3.3. Maximizing warehouse space utilization:

There exist various strategies for expanding the use of extra room.

The unitization issue has been examined by Steudal (1979), his goal being to parcel the bed into more modest indistinguishable rectangular regions in order to limit the measure of unused bed region. This is an exceptional instance of the two-dimensional cutting stock issue which permits non-guillotine cuts. Steudal first uses dynamic programming to decide the ideal arrangement of the little square shapes along within edge of the bed. In the econd stage, the ideal plan of square shapes along the edge of the bed is projected internal to fill in the middle portion. Interference can be checked for by assessing straightforward direct limitations, and afterward diminished.

Tsai, Malstrom and Meeks (1988) address the utilization of straight programming to decide an ideal answer for a comparable issue, then again, actually they permit a wide item blend of various box sizes to be stacked on a similar bed. Square stacking is utilized for putting away enormous amounts of palletized or boxed items on top of one another in stacks, without racks. Generally, forklift trucks are utilized to control the beds each in turn. A capacity path stays inaccessible for showing up beds until its present substance has been completely drained by request, accordingly making the need to streamline capacity path profundity.

Bog (1979) fostered a GPSS reproduction model to explore the impact of substitute path profundities on space usage, utilizing factual investigation to decide whether they essentially impact execution measures like essential stockpiling region and lineal walkway facade.

Goetschalckx and Ratliff (1991) portray a powerful programming calculation for a solitary item and number numerous path profundities, the states and phases of which compare to the length and number of capacity paths, individually. Heuristics are portrayed for the situation where path profundities are confined to a limited set because of reasonable execution contemplations.

3.3.1. Minimizing order picking costs:

The soonest devoted capacity calculation is the block per-request list (COI) rule of Heskett (1963), where the COI of a thing is characterized as the proportion of the thing's complete expected space to the quantity of outings needed to fulfill its interest. The algorithm consists of finding the things with the most minimal COI nearest to the P/D point, that is, those things which consolidate a high turnover recurrence with a low space prerequisite. Things are then relegated to areas continuously farther away from the P/D point by expanding COI.

Albeit the COI algorithm was at first considered as a heuristic, Harmatuck (1976) showed that it yields an ideal answer for the specific numerical programming definition of a similar issue, expecting a solitary order framework, single-request picking, and that the movement autonomy condition holds.

The last suggests that the expense of moving all things is consistent and corresponding to the distance voyaged. The optimality of the COI algorithm was subsequently approved for double order frameworks by Malmborg and Krishnakumar (1987).

Francis and White (1974) demonstrated that a similar algorithm is again ideal on account of a multi-dock office, given that all things have a similar likelihood mass capacity for determination of a dock.

Jarvis and McDowell (1991) inferred some stock area algorithms for a request picking stockroom having the very construction as that portrayed in Ratliff and Rosenthal (1983), that is, a solitary square of equal walkways with cross-overs just at the closures of the passageways.

5. Warehouse design models:

5.1. Internal arrangement:

Bozer (1985) creates execution models for in-the-walkway picking versus end-of-passageway picking under arbitrary capacity, with the target of limiting expense subject to throughput and extra room imperatives. Insightful articulations are utilized sooner rather than later, while Monte Carlo testing and relapse investigation are needed for the immovable cases, especially end-of-passageway frameworks. The compromise among picking and save stockpiling regions was additionally considered by Bozer. This compromise can be expressed as the increment in picking time versus the decline in renewal recurrence (from hold region to picking region) as the picking region is expanded. End-of-walkway picking was again dissected by Bozer and White (1990). It was tracked down that the necessary number of walkways increments as the passageways become less square (on schedule), and that the throughput limit is roughly direct in the quantity of paths. Positioning elective region tasks was refined with multi-trait esteem works by Pliskin and Dori (1982).

Through unequivocal thought of compromises among four space classifications, the procedure creates a position requesting steady with the leader's inclinations. In the examination there is a cutoff to the measure of room accessible, an increment in the portion to one sort of room being balanced by a lessening in different assignments. The issue of designating scant floor space between an arbitrary access region and a rack stockpiling region was demonstrated by Azadivar (1989).

Irregular access extra rooms are those which are haphazardly open by the material taking care of framework, yet not by the S/R machine. Then again, rack stockpiling requires the utilization of the S/R machine and accordingly takes additional time, bringing about the development of lines.

Perry, Hoover and Freeman (1984) report on a model to aid the improvement of plan heuristics for an AS/RS. The throughput limit of the AS/RS is first assessed expecting deterministic conditions, which gives beginning qualities to the plan factors. Ideal looking for rules dependent on the thought of steepest rising of a reaction surface are then utilized inside a reproduction model to get a nearby ideal for the quantity of stacker cranes and the quantity of workstations.

5.2. Overall design:

A rectangular stockroom plan issue was considered by Francis and White (1974). They accept that warehouse region and stature are foreordained amounts, that there is a solitary shipping bay, that things areequally liable to move between the harbor and any point in the stockroom, and single-order load dealing with. The issue is displayed as a persistent format, and the expense work is to such an extent that a logical arrangement is determined.

Bassan, Roll and Rosenblatt (1980) analyze two elective rack courses of action, accepting that all pieces of the distribution center are similarly logical of being used, and that the stockroom is rectangular, with the passage and leave entryways situated on inverse longitudinal dividers. All expenses have a place with one of the accompanying classes: material taking care of cost (accepting rectilinear travel), yearly expense per unit of distribution center region, and yearly expense per unit length of outer dividers. The investigation yields the ideal number of extra rooms along a rack, number of twofold retires, area of entryways, and distribution center measurements.

Karasawa, Nakayama and Dohi (1980) introduced a non-straight blended whole number definition for the ideal plan of a solitary order AS/RS, joining cost parts for racks, cranes, building and land. Limitations incorporate adequate crane ability to meet required assistance levels, and satisfactory volume to store expected stock levels accepting an arbitrary stockpiling strategy.

Choice factors are the quantity of cranes required (whole number), and the tallness and length of the stockroom (genuine). The ideal arrangement is found by the Lagrange multiplier strategy. An enhancement model for the plan of

a double order AS/RS was proposed by Ashayeri, Gelders and Van Wassenhove (1985). The general extents of the different target work terms and the convexity of the target work in the quantity of walkways permit a one-dimensional consecutive pursuit over the quantity of paths to yield an ideal arrangement.

Park and Webster (1989) think about elective warehousing frameworks based on the accompanying elements: control methodology, dealing with hardware development, stockpiling task rules, info and yield designs for item stream, stockpiling rack structure, part costs and the financial matters of every capacity framework. Every option is created and analyzed by a comprehensive count measure the goal being to limit absolute yearly expenses, travel time, as well as land necessities.

Rosenblatt, Roll and Zyser (1989) introduced a recursive advancement recreation heuristic for acquiring ideal plan boundaries for an AS/RS, given pre-determined limits on some presentation measures. A number non-straight model builds up the actual qualities of the AS/RS with the goal of limiting introductory and intermittent expenses over its financial life while overlooking the unique idea of the framework. Results from the advancement are taken care of into a reenactment model from which the exhibition measures can be assessed. A relationship dependent on various direct relapse is then characterized between the plan factors and the exhibition measures.

At last this relationship is fused as an imperative into the following execution of the improvement model, etc, until a satisfactory outcome is accomplished.

6. Mathematical model for warehouse design and product allocation:

6.1. Model assumptions:

This parte considers warehouse designs that incorporate a subset of the accompanying five useful regions: getting, delivering, organizing for cross-docking activity, save and forward. In the getting region, bed burdens or individual containers of items are gotten. On the off chance that essential, they are arranged for a brief period and moved either to the transportation region straightforwardly (cross-docking activity) or to the capacity region.

In the transportation region, picked request things are prepared (for example contract wrapped, stuffed) and arranged (if essential) for transportation to the following objective. In the organizing region for cross-docking, items are arranged and amassed for additional outbound activities. The hold region is a capacity region for cumbersome item things that commonly live in the stockroom for a moderately longer length. Regularly, the hold region utilizes high-thickness stockpiling gear to accomplish the objective of high space usage.

The forward region is a somewhat more modest stockpiling region ordinarily utilized for quick request picking or performing esteem added activities or request assemblage. Along these lines, the accompanying material streams are conceivable in a stockroom (figure 1):

- . Flow 1: Receiving → cross-docking → shipping.
- . Flow 2: Receiving → reserve area → shipping.
- . Flow 3: Receiving → reserve area → forward area → shipping.
- . Flow 4: Receiving → forward area → shipping.

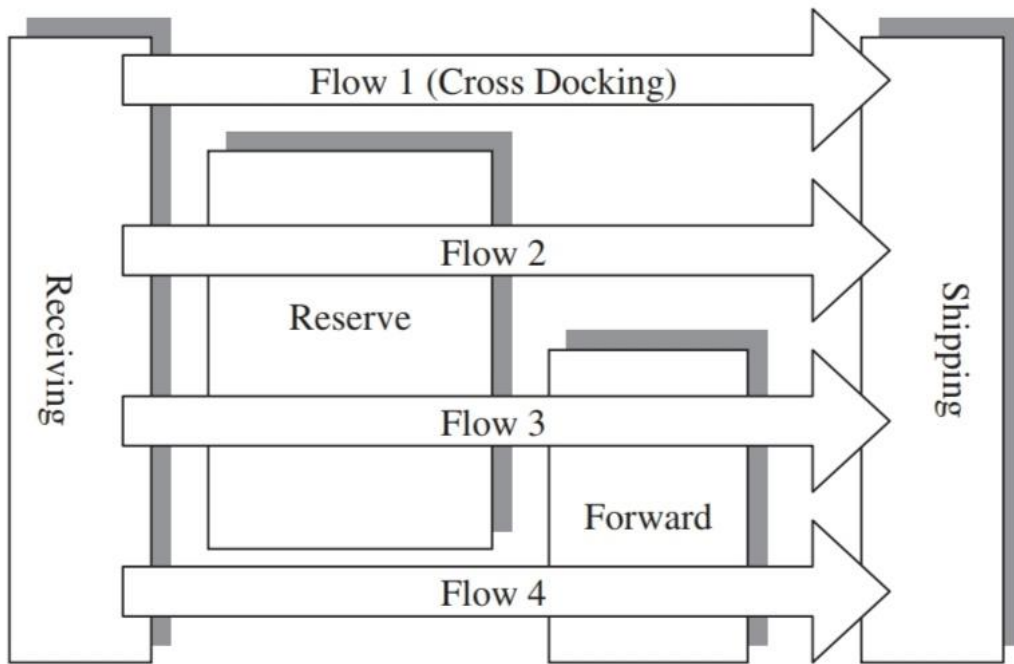


Figure 1. Typical product flows in a warehouse.

Flow 1 is the cross-docking operation. Upon receipt, product items are either put into a staging area for a short period and then moved to the shipping area, or directly moved to the shipping area. The received products are typically presorted at suppliers' facilities. The operation here is simply to pass on the product to a customer or the next facility in the supply chain. A number of companies use this strategy for efficient operation and management of the supply chain.

Flow 2 is a typical warehouse operation. Products are stored in a reserve area and order-picking operation is performed as required. It is assumed that, typically, only those items that remain in the warehouse for relatively extended periods and shipped as is (or with minimal value added operations) will be allocated to the reserve storage area.

Flow 3 is also a typical warehouse operation. Products are first stored in the reserve area typically in pallet loads, broken into smaller loads (cartons or cases) and then moved to the forward area for fast order picking, order consolidation or performing value added operations.

Flow 4 can be thought of as another form of cross-docking operation. Products are received and then are directly put into forward area to perform the order consolidation. This type of operation is usually seen in the supplier warehouses or when there is a need to consolidate large orders.

The next section presents a mathematical model that determines the flow to which each product must be assigned and as result, the size of the functional areas within the warehouse. It assumes the following:

- . Available total storage space is known.
- . Expected time a product spends on the shelves is known. This is referred to here as the dwell time.
- . Cost of handling each product in each flow is known.
- . Dwell time and cost have a linear relationship.

. Annual product demand rates are known.

. Storage policies and material-handling equipment are known and these affect the unit handling and storage costs.

6.2. Model formulation:

In formulating the model, the following notation is used.

Parameters:

- i number of products, $i = 1, 2, \dots, n$,
- j type of material flow, $j = 1, 2, 3, 4$,
- λ_i annual demand rate of product i in unit loads,
- A_i order cost for product i ,
- P_i price per unit load of product i ,
- p_i average percentage of time a unit load of product i spends in reserve area if product is assigned to material flow 3,
- $q_{ij} = 1$ when product i is assigned to material flow $j = 1, 2$ or 4; $[d_i] = 1$ when product i is assigned to flow $j = 3$, where d_i is the ratio of the size of the unit load in reserve area to that in forward area and $[d_i]$ is the largest integer greater than or equal to d_i ,
- a, b, c levels of space available in the vertical dimension in each functional area,
 $a =$ cross-docking, $b =$ reserve and $c =$ forward,
- r inventory carrying cost rate,
- H_{ij} cost of handling a unit load of product i in material flow j ,
- C_{ij} cost of storing a unit load of product i in material flow j per year,
- S_i space required for storing a unit load of product i ,
- TS total available storage space,
- Q_i order quantity for product i (in unit loads),
- T_i dwell time (years) per unit load of product i ,
- LL_{CD}, UL_{CD} lower and upper storage space limit for the cross-docking area,
- LL_F, UL_F lower and upper storage space limit for the forward area,
- LL_R, UL_R lower and upper storage space limit for the reserve area.

Decision variables:

- X_{ij} 1 if product i is assigned to flow type j ; 0 otherwise,
- α, β, γ proportion of available space assigned to each functional area,

α = cross-docking, β = reserve and γ = forward.

Model 1:

$$\text{Min } 2 \sum_{i=1}^n \sum_{j=1}^4 q_{ij} H_i \lambda_i X_{ij} + \sum_{i=1}^n \sum_{j=1}^4 \left(\frac{q_{ij} c_{ij} Q_i X_{ij}}{2} \right) \quad (1)$$

$$\sum_{j=1}^4 X_{ij} = 1 \quad \forall i \quad (2)$$

$$\sum_{i=1}^n \left(\frac{Q_i S_i X_{ij}}{2} \right) \leq a \alpha T S \quad (3)$$

$$\sum_{i=1}^n \left(\frac{Q_i S_i X_{i2}}{2} \right) + \sum_{i=1}^n \left(\frac{p_i Q_i S_i X_{i3}}{2} \right) \leq b \beta T S \quad (4)$$

$$\sum_{i=1}^n \left(\frac{(1-p_i) Q_i S_i X_{i3}}{2} \right) + \sum_{i=1}^n \left(\frac{Q_i S_i X_{i4}}{2} \right) \leq c \gamma T S \quad (5)$$

$$\alpha + \beta + \gamma = 1 \quad (6)$$

$$LL_{CD} < a \alpha T S < UL_{CD} \quad (7)$$

$$LL_R < b \beta T S < UL_R \quad (8)$$

$$LL_F < c \gamma T S < UL_F \quad (9)$$

$$\alpha, \beta, \gamma \geq 0 \quad (10)$$

$$X_{ij} = 0 \text{ or } 1 \quad \forall i, j. \quad (11)$$

The dwell time is the average duration a product stays on the shelf and is assumed to be known or can be estimated by the warehouse manager. In fact, based on annual product demand λ_i , order cost A_i , price per unit load of product P_i and carrying cost rate r , a simple economic order quantity (EOQ) model can be used to determine the optimal order quantity Q_i , as well as the average time a unit load of product spends on the shelves. For example, since the time between two successive replenishments is Q_i/λ_i , the average dwell time per unit load of product i is $T_i = Q_i/(2\lambda_i)$. Note that $Q_i/2 = \lambda_i T_i$ and this value or another reasonable estimate must be used in the objective function (1), which minimizes the total cost of handling the average, annual loads of each product assigned to its respective area as well as the corresponding annual storage costs. The reader should not confuse storage costs with inventory holding costs.

While inventory holding costs depend only upon the value of the inventory, they are the same whether the inventory is in reserve or forward or cross-docking area. Storing costs, on the other hand, depend upon the area in which the product is stored and these costs tend to carry a premium for the cross-docking and forward areas (because these are considered prime real estate in a warehouse) and are relatively not that expensive for the reserve area. Of course, the handling costs are different (in fact, the opposite) for these areas and thus our model trades off storage costs against handling costs. Note that X_{ij} tells us whether or not product i is assigned to flow j , and $Q_i X_{ij}/2$ gives the average number of the corresponding unit loads in inventory.

The model implicitly assumes that the unit load size for each product is not dependent upon the flow to which the product is assigned. In general, the size of a unit load for a product i that remains in one area is equal to that received from the supplier. The exception is for products assigned to flow 3 because these products have different unit load sizes in the two areas encompassing flow 3. The unit load size of products assigned to flow 3 could be equal to that received from the suppliers in the reserve area, but different when handled in the forward area.

This occurs because a pallet load is broken down to cases or cartons in the forward area. This is only for products assigned to flow 3. Hence, we introduce d_i to denote the ratio of the size of the unit load in the reserve area to that in the forward area and q_{ij} for $j = 3$ accounts for the fact that product i is handled $[d_i] + 1$ times.

H_{ij} and C_{ij} should therefore correspond to aggregate handling and storage costs for $j = 3$. The model also implicitly assumes that for a product assigned to flow 3, the unit load size decreases as it moves from the reserve to forward area. If necessary this assumption can be relaxed and a more general model can be developed rather easily.

The model also assumes that each product incurs two material-handling transactions, one for receiving and another for shipping, regardless of the area to which it is assigned. If products assigned to a particular flow require more than two (or only one) material-handling transactions, the coefficient of the corresponding terms in the objective function must be appropriately weighted. For example, in some cases, the products assigned to the combined forward/reserve flow may incur three transactions, one for receiving at the reserve area, another for shipping to forward area and a third for shipping. If this is the case, that term must have a

coefficient of 3. Constraint (2) ensures that each product is assigned to only one type of material flow. If the same product could be allocated to multiple flows due to different demand patterns, then our model requires that the manager at least knows

or can estimate the percentage of this product that could be assigned to two or more of the four flows. For modelling purposes, additional versions of this product are then created (depending upon how many flows this product could be assigned to) with the demand data appropriately reduced. For example, assume that 70% of a certain product whose demand is a 10 000 units per year on average is likely to be assigned to one of the four flows, say reserve storage and another 30% to another, say cross-docking. For modelling purposes, an additional version of this product is

therefore created with demand equal to 7000 and 3000 for the two products. Note that although the manager might assume that the product is likely to be split on a 7:3

ratio to reserve:cross-docking, the model may provide a different assignment based on the total costs. Constraints (3)–(5) ensure that the space constraints for the crossdocking, reserve and forward areas are met. The right-hand side includes three additional variables whose sum is required to be 1 (constraint 6). This is to ensure 100% of the space available is allocated to the three areas. Constraints (7)–(9) serve to enforce upper and lower limits on the space that can be allocated to cross-docking, forward and reserve areas.

We believe much of the input data such as the type and number of products, annual demand for each, order cost, unit price, carrying cost rate, etc., are readily available to the warehouse designer. The storage cost C_{ij} is typically a function of the size of a product's unit load, warehouse leasing/construction costs per square foot, as well as the type of shelving used in each area encompassing flow j . C_{ij} and H_{ij} for flow 3 must be aggregated to account for the fact that a pallet load could be broken down into cases or cartons. The cost of handling a unit load of product i in each flow j is a function of the product size, its handling characteristics as well as the material handling system used in the area(s) included in flow j . Tamashunas et al. (1990) provide a simple formula to estimate these costs based on labour, non-labour as well as prorated capital recover costs of the material-handling system. This formula is adapted to the warehouse application using the following

additional notation:

IC_j investment or leasing cost of material-handling device cost in flow j ,

- L_j average percentage of time material-handling device in flow j travels loaded,
- SP_j average speed of material-handling device in flow j (feet/min),
- OP_j labour and non-labour cost to operate material-handling device in flow j (per min),
- LUL_{ij} average loading and unloading time in minutes for product i using material-handling device in flow j ,
- d_{ij} average distance travelled to store or retrieve product i in flow j ,
- N_{ij} average number of unit loads of product i handled in flow j .

$$H_{ij} = \frac{TC_{ij}}{N_{ij}}, \text{ where} \tag{12}$$

$$TC_{ij} = (IC_j) \frac{N_{ij} \left(LUL_{ij} + \left(\frac{d_{ij}}{L_j SP_j} \right) \right)}{\sum_{i=1}^n N_{ij} \left(LUL_{ij} + \left(\frac{d_{ij}}{L_i SP_j} \right) \right)} + N_{ij} (OP_j) \left(LUL_{ij} + \frac{d_{ij}}{L_i SP_j} \right). \tag{13}$$

Note that the first part of (13) prorates the investment or leasing cost of the material-handling device (assigned to a flow) to each product and the second part assigns the operating costs. Dividing this term by the number of unit loads of the product assigned to the flow under consideration, it estimated the per unit load handling cost. The only disadvantage with this method is that it requires knowledge of the product assignment to each flow, the main decision variable in the mathematical model (1)–(11). To overcome this disadvantage, we recommend that the decision-maker uses this model in two passes. First, assuming some initial assignment of products to flows, calculate the H_{ij} values. Use these values to solve the model. Based on the product assignment obtained from the model, change the H_{ij} values and resolve the model.

As will be seen in the experimental section, Model 1 may require much computation time, especially for large-scale problems. To solve large-scale problems, we modify the bounds or change the inequalities to equalities. Two such modified models are shown below.

Model 2 :

$$\text{Min } 2 \sum_{i=1}^n \sum_{j=1}^4 q_{ij} H_i \lambda_i X_{ij} + \sum_{i=1}^n \sum_{j=1}^4 \left(\frac{q_{ij} C_{ij} Q_i X_{ij}}{2} \right) \tag{1}$$

subject to (2)–(5), (7)–(11) and

$$\alpha + \beta + \gamma \leq 1 \tag{14}$$

$$LL_{CD} = LL_R = LL_F = 0 \tag{15}$$

Model 3 :

$$\text{Min } 2 \sum_{i=1}^n \sum_{j=1}^4 q_{ij} H_i \lambda_i X_{ij} + \sum_{i=1}^n \sum_{j=1}^4 \left(\frac{q_{ij} C_{ij} Q_i X_{ij}}{2} \right) \tag{1}$$

subject to (2), (7)–(11), (14)–(15) and

$$\sum_{i=1}^n \left(\frac{Q_i S_i X_{ij}}{2} \right) = a\alpha TS \quad (16)$$

$$\sum_{i=1}^n \left(\frac{Q_i S_i X_{i2}}{2} \right) + \sum_{i=1}^n \left(\frac{p_i Q_i S_i X_{i3}}{2} \right) = b\beta TS \quad (17)$$

$$\sum_{i=1}^n \left(\frac{(1-p_i) Q_i S_i X_{i3}}{2} \right) + \sum_{i=1}^n \left(\frac{Q_i S_i X_{i4}}{2} \right) = c\gamma TS \quad (18)$$

6.3. Heuristic algorithm:

Although large instances of the warehouse design model can be solved directly using an available branch-and-bound-based algorithm for mixed-integer programming problems (tables 1 and 2), when the problem is severely constrained so that there are a limited number of feasible solutions, or when the number of products is in the hundreds of thousands, the number of binary integer variables increases considerably and solving the resulting model takes significant computational time. Hence, proposed below is an efficient heuristic for solving the model.

Heuristic algorithm:

Step 1. For each $i=1, 2, \dots, n$, find $\min_{j=1, 2, 3, 4} (2q_{ij}H_{ij}\lambda_i + q_{ij}C_{ij}Q_i/2)$.

Let $\min_{j=1, 2, 3, 4} (2q_{ij}H_{ij}\lambda_i + q_{ij}C_{ij}Q_i/2)$ occur for $j = j^*$.

Set $X_{ij^*} = 1$, remaining $X_{ik} = 0$, $k = 1, 2, 3, 4$, $k \neq j^*$.

Step 2. Calculate α , β , and γ using equations (16–18). If $\alpha + \beta + \gamma > 1$, stop because the problem is infeasible. Otherwise, go to Step 3.

Step 3. Calculate the upper bound on α , β , and γ as follows:

$$\alpha_{UB} = UL_{CD}/aTS; \quad \beta_{UB} = UL_R/bTS; \quad \text{and} \quad \gamma_{UB} = UL_F/cTS.$$

If $\alpha \leq \alpha_{UB}$, $\beta \leq \beta_{UB}$, and $\gamma \leq \gamma_{UB}$, stop because there is a feasible, optimal solution. Otherwise, go to Step 4.

Step 4. Let $\max \{ \alpha - \alpha_{UB}, \beta - \beta_{UB}, \gamma - \gamma_{UB} \}$ occur for area k , $k = 1, 2, 3$, and

$\min \{ \alpha - \alpha_{UB}, \beta - \beta_{UB}, \gamma - \gamma_{UB} \}$ occur for area l , $l = 1, 2, 3$. Set $k^* = k$, $l^* = l$, place k^* in set P , l^* in set Q , and the remaining index m in set P if the area's total space coefficient exceeds the corresponding upper bound. Otherwise, place the remaining index m in set Q .

Step 5. Pick a product i^* in area k^* and place it in area l^* provided:

- (i) the upper bound space constraint in area l^* is not violated, and
- (ii) $(2q_{il^*}H_{il^*}\lambda_i + q_{il^*}C_{il^*}Q_i/2) - (2q_{ik^*}H_{ik^*}\lambda_i + q_{ik^*}C_{ik^*}Q_i/2)$ is minimum for $i = i^*$.

If no product satisfying conditions (i) and (ii) exists, set $k^* = m$ and repeat Step 5. If no product satisfying conditions (i) and (ii) exists, stop, because no feasible solution is found

Step 6. If the current solution is feasible stop. Otherwise, repeat Step 2.

Several aspects of the above algorithm are worth discussing. First, it is easy to show that the solution obtained in Step 1 is optimal for the model in Section 4 excluding the space constraints (3)–(10). If such a solution does not exceed

the upper bounds on the three total space coefficients α_{UB} , β_{UB} , and γ_{UB} , then it is an optimal solution to Model M1 (see Step 3). Thus, the solution obtained at the end of Step 1 provides a very tight lower bound on the objective function value for the model specified by constraints (1)–(11). It is thus no surprise that the general-purpose branch-and-bound algorithm in LINDO can solve problems with 15 000 products. Second, no feasible solution may be available at the end of Step 2.

It can be shown that if $\alpha + \beta + \gamma > 1$, then no feasible solution to the problem can be developed without increasing the total space (TS). Third, Step 4 places the areas for which the total space coefficient exceeds the corresponding upper bound in set P and the others in set Q. Only three areas—cross-docking, reserve and forward—are considered here, so the two sets can have only three elements. Step 5 examines the area for which the total space coefficient exceeds the corresponding upper bound the most and transfers it to the area with the most available space, i.e. the area in set Q.

Note that the space constraint is not violated for the areas belonging to set Q. Fourth, if the heuristic algorithm cannot transfer products from one of the areas in set P to another in set Q according to the two conditions in Step 5, it terminates because it cannot find a feasible solution. Otherwise, Steps 2–5 are repeated until a feasible solution is found. Whenever the heuristic algorithm cannot find a feasible solution, we recommend that the total space be increased and the problem resolved. Fifth, instead of terminating the heuristic after finding a feasible solution in Step 6, one could apply the simulated annealing algorithm using the procedure outlined in Heragu (1997).

The simulated annealing algorithm systematically considers swapping a product currently assigned to flow j to another flow as well as swapping pairs of assignments provided such an exchange yields a feasible solution. For example, if product i is assigned to flow p and j is assigned to flow q, the algorithm considers assigning product i to flow q and j to flow p.

7. Planning of warehouse operations:

In this segment we center around the capacity area relegate mint issue at the strategic level. The techniques that are created at this level, fill in as a system for the genuine area determination for approaching products. In these systems, the conduct on the transitional term is assessed by chronicled request designs. Since the capacity area task issue will be immovable overall, we present the progressive Storage Location Planning Procedure.

7.1. Distribution of products among warehousing systems:

Most large warehouses contain more than one type of warehousing system. Each warehousing system is especially equipped for a specific group of products based on their characteristics, such as: size, weight, shape, perish-ability, volume, demand rate, pick sizes, delivery quantity, type of storage module, et cetera. Furthermore, many warehouses use separate systems or areas for order-picking (forward area) and for bulk storage (reserve area). Whenever a product in the forward area has been depleted, it is replenished from the reserve area. A well-known forward-reserve configuration is a storage rack where the lower levels are used for manual order-picking (forward area) and the higher levels contain the bulk storage (reserve area).

. The authors assume that one replenishment trip suffices to replenish a product, irrespective of the allocated quantity. The authors derive analytic expressions for the optimal product quantities as a function of the available storage space. They present a knapsack-based heuristic that assigns these quantities to the forward area in sequence of decreasing cost savings until it is full.

Frazelle incorporate the heuristic into a framework for determining the optimal size of the forward area. The costs in the model for order-picking in the forward area and for replenishing are related to the size of the forward area. Furthermore, they impose a congestion constraint and show its redundancy. Clearly, a model that minimizes the activity in the forward area, may well minimize the congestion at the same time. They prove that the procedure in Hackman and Rosenblatt gives an optimal solution to the continuous relaxation of the problem.

Finally, Frazelle present a case study where they project a 20% saving on labor cost by re-sizing the forward area down to 32% of its original size and by re-allocating the products among the forward and reserve area. Van den Berg consider a warehouse with busy and idle periods where reserve-picking is possible. Their model allows advance replenishments during idle periods to reduce the replenishment activity during subsequent busy periods. This not only increases the throughput during the busy periods, it also reduces congestion and accidents. Contrary to the above publications, consider a situation (e.g. pallet storage) where only one load is replenished per trip. The authors present a knapsack-based heuristic with a tight performance guarantee that attempts to find an allocation of products to the forward area that minimizes the total expected amount of work related to order-picking and replenishing during a busy period. Experiments with random data show savings may be possible of up to 30% in comparison with procedures used in practice.

7.2. Balancing of workload within a warehousing system:

In numerous tasks, request pickers are devoted to zones to diminish blockage and travel time. In such circumstances we might build the throughput limit by circulating the (bunches of) items among the zones with the end goal that the van nook Berg mean and pinnacle responsibility are adjusted among zones. In like manner, in an AS/RS with various passageways a S/R machine in every walkway, we might work on the limit of the framework by circulating the responsibility equitably among the S/R machines. We don't know about any distributions examining this issue regarding warehousing.

7.3. Task of items to capacity areas:

The Storage Location Assignment Problem (SLAP) concerns the assignment products to storage locations. Such an assignment establishes a framework for allocating incoming loads to storage locations.

Hausman present three storage location assignment policies: randomized storage, class-based storage and dedicated storage. The randomized storage policy allows products to be stored anywhere in the storage area. The class-based storage policy distributes the products, based on their demand rates, among a number of classes and for each class it reserves a region within the storage area. Accordingly, an incoming load is stored at an arbitrary open location within its class. Under the dedicated storage policy each location may only be used for a specific product. Randomized and dedicated storage are in fact extreme cases of the class-based storage policy: randomized storage considers a single class and dedicated storage considers one class for each product. Class-based storage and dedicated storage attempt to reduce the mean transaction times for order-picking by storing products with high turnover at locations that are easily accessible. Randomized and class-based storage are also known as shared storage policies, for these allow the successive storage of units of different products in the same location.

8. Control of warehousing operations:

The planning policies define a framework under which the control of warehousing operations takes place. Some control problems in warehousing systems are:

- Batching of orders.
- Routing and sequencing.
- Dwell point positioning
- Dynamic control of warehouses

8.1. Routing and sequencing:

In this section we discuss routing and sequencing in warehousing systems. In Section 8.1.1 we consider unit-load retrieval systems. Subsequently, in Section 8.1.2 we discuss order-picking systems. Finally, in Section 8.1.3 we observe carousel systems.

8.1.1. Unit-load retrieval operations:

The sequencing of storage/retrieval requests in an AS/RS has received extensive attention in the literature. Hausman just consider single order cycles. Graves study the impacts of performing double order cycles. They notice travel time decreases of up to 30%. Han et show that the AS/RS throughput performance might be improved by cunningly sequencing the recovery demands, so the interleaving travel time among capacity and recovery areas in a double order cycle is decreased. The noticed time investment funds rely upon the quantity of open areas in the racks and the quantity of accessible stockpiling and recovery demands.

Han et al. propose the notable closest neighbor rule for discovering a grouping of capacity and recovery re-missions under the static methodology. They additionally examine the no expense zone for the Chebyshev metric, i.e., the region in the rack that might be visited for a capacity without extra (Chebyshev) travel time, while going from the information station to a recovery area. In light of this, they present the most brief leg heuristic. In any case, this heuristic was outflanked by the closest neighbor heuristic because of the way that it seemed to top off the space near the I/O station.

Lee and Schaefer utilize a Linear Assignment Problem (LAP) to take care of the sequencing issue when there is an equivalent number of capacity and recovery demands. It might happen that the arrangement of the Linear Assignment Problem relates to an infeasible grouping since an area is to be utilized for capacity while the item won't have been recovered at this point. The creators utilize the positioning calculation of Murty which dully tracks down the following best arrangement of the LAP. Since this may require over the top calculation times until a plausible arrangement is discovered, they force a breaking point on the quantity of emphases and apply a heuristic that builds an achievable arrangement at every cycle.

Lee and Schaefer show that under the devoted stockpiling strategy the LAP sets up an ideal answer for the static methodology. Stretching out the static way to deal with a powerful circumstance (settling the LAP after every modification of the request set) does not give great outcomes since it was beaten by a basic avaricious heuristic. Moreover, they show that the unique methodology builds up normal investment funds of 10-20% of the interleaving time contrasted with the static methodology. Van sanctum Berg likewise thinks about the committed stockpiling strategy and tackles the issue to optimality in polynomial time by displaying it as a Transportation Problem.

The model is an augmentation of Lee and Schaefer since it permits subjective places of the info and yield stations and any quantities of capacity and recovery demands. Lee and Kim consider the issue of limiting earliness and lateness punishments when all stockpiling and recovery demands have a typical due date. A few reenactment studies have been introduced of an AS/RS for the powerful methodology, including those of Schwarz, Linn and Wysk, Seidmann and Linn and Xie.

Schwarz validate the identicalness of the Closest Open Location (COL) rule and randomized stockpiling under reasonable conditions. Additionally, they analyze the mean process duration of the nearest open area decide to that of the class-based capacity strategy, with a few classes, while considering interleaving and diverse line lengths of recoveries pausing. At last they consider defective data on the turnover paces of items. They track down that the class-based capacity strategy can endure genuinely enormous blunders in the turnover rate front projecting without expanding the mean process duration consider-capably.

Linn and Wysk methodically assess various capacity and recovery choice standards when the item request shows occasional pattern.

Seidmann presents a powerful control approach that alters its arrangements dependent on the quantity of solicitations pausing and changes in turnover rate. Linn and Wysk present a specialist framework that adjusts its controls relying upon the use pace of the AS/RS. Linn and Xie think about an AS/RS in a gathering climate. To forestall delay in the get together, earnestness decides are utilized that offer need to capacity and recovery demands that are near their given due dates.

Keserla and Peters and Sarker consider an ASIRS with SIR machines that have double transports. This permits two stockpiles and two recoveries for every cycle. Also, one stockpiling might be performed following an area has been cleared by a recovery. For a broad survey of movement time models in AS/RS's we allude to Sarker and babu.

8.1.2. Order picking operations:

Ratliff and Rosenthal present a powerful program-ming calculation that takes care of the Traveling Salesman Problem (TSP) in an equal passageway stockroom with get over paths at the two finishes of every walkway. The calculation season of this calculation is direct in the quantity of stops. They guarantee that the issue stays manageable in case there are three hybrids for every walkway. Petersen assesses the presentation of five directing heuristics in examination with the calculation of Ratliff and Rosenthal .

The best heuristics were on normal 10% over ideal for different stockroom shapes, areas of the I/O station and pick list sizes. Indeed, even awesome of the five arrangements was on normal 5% over the ideal arrangement.

Goetschalckx and Ratliff give a proficient algorithm for request picking in a distribution center with no negligible walkway width. In wide paths two way travel is conceivable, traffic can turn and pass and it is feasible to utilize fork lifts for picking. It gave the idea that reserve funds of up to 30% are conceivable by picking the two sides of the passageway in a similar pass instead of picking one side first and getting back to pick the opposite side.

Goetschalckx and Ratliff consider the issue of deciding the ideal stop places of a request picking vehicle in a path when the request picker is permitted to play out various picks per stop. They propose an effective unique programming calculation for the in-position that the movement season of the request picker is estimated with the rectilinear measurement. The issue of sequencing picks for a man-on board 5/R machine activity in one path is a case of the TSP with the Chebyshev or rectilinear measurement, contingent upon the movement qualities of the crane.

Gudehus depicts the generally utilized band heuristic. This heuristic partitions the rack into two even groups. First the areas on the lower band are visited on expanding x-facilitate, thusly the areas on the upper band are visited on diminishing x-arrange. Any significantly, number of groups can be utilized, but two groups give the best outcomes for up to 25 picks. The raised body of a bunch of hubs is the littlest arched region that incorporates all hubs. Brilliant and Stewart examine the property that each TSP for which travel times are estimated by the Euclidean measurement has an ideal arrangement wherein the hubs on the limit of the arched structure are visited in a similar succession as though the limit of the curved body itself were followed.

The Euclidean metric or L2-standard is characterized as: $\sqrt{A_x^2 + A_y^2}/v$, when A_x and A_y indicate the interpretations in flat and ran nook Berg vertical bearing, individually, and v signifies the movement speed.

Akl and Toussaint present a quick calculation for tracking down the curved body. Allison and Noga demonstrate the property for the rectilinear measurement and Goetschalckx for the Chebyshev metric. The rectilinear measurement or L_1 - standard is characterized as: $a_x e + A_y/17$, when A_x and b_y de-note the interpretations level and vertical way, individually, and e and indicate the movement speeds flat and vertical way, separately. Note that Chebyshev venture out is identical to rectilinear travel with the arrangement of tomahawks pivoted more than 45 degrees.

Bozer present a heuristic that utilizes the curved frame of the rack areas as an underlying sub tour. In this way, the areas in the inside of the arched body are embedded. For the Chebyshev and the rectilinear metric some locations can be embedded without expanding the movement time.

Bozer additionally present a further developed adaptation of the band heuristic that squares out a focal part of the rack. The band heuristic is executed for the leftover areas, after which areas in the impeded region are embedded. In the wake of building the visit, 2-select and 3-pick nearby trade schedules are applied which endeavor to lessen the visit length.

Hwang and Song consider the circumstance where the request picking truck performs Chebyshev travel under a foreordained tallness, over this stature it embraces recti-straight travel to guarantee the security of the request picker. They present a heuristic that considers the curved body for Chebyshev travel and rectilinear body for rectilinear travel.

Daniels consider the circumstance where items are put away at various areas and the pick area for an item might be chosen from any of these areas. Such a methodology frequently won't be satisfactory for the accompanying two reasons. Initially, it proliferates maturing of the stock, since items are not really recovered by a First In First Out (FIFO) strategy. Notwithstanding, in any event, for non-crumbling things this regularly is not attractive. Besides, it expands the extra room prerequisites, since there will be different deficient beds in the distribution center each occupying a total stockpiling area. They present six heuristics and a lower bound. A few heuristics perform near the below all things considered.

8.1.3. Carousel operations:

The pick sequencing issue in merry go round frameworks has gotten significant consideration in the writing. Bartholdi and Platzman consider sequencing of picks in a solitary request. They expect that the time required by a (automated) picker to move between containers inside a similar transporter (or rack) is irrelevant contrasted with an opportunity to turn the merry go round to the following transporter (or rack). This supposition diminishes the issue to tracking down the most limited Hamiltonian way on a circle. They present a straight time calculation that tracks down an ideal arrangement. Wen and Chang additionally consider sequencing picks in a solitary request. They accept that an opportunity to move between containers inside a similar transporter or rack may not be dismissed. They present three heuristics for the present circumstance, in view of the calculation in Bartholdi and Platzman.

A few creators have considered the circumstance where the request picker successively picks various orders in this way finishing all picks in a request prior to beginning with the following request, i.e., all picks in a request are performed continuously. Ghosh and Wells and van sanctum Berg present effective powerful programming calculations that track down an ideal pick grouping for picking different orders when the arrangement of the orders is fixed (the sequence of the picks in the orders is free).

Bartholdi and Platzman consider the issue when the request sequence is free, yet picks inside a similar request should be performed successively. They force the additional constraint that each request is picked along its briefest range Ning span, and present a heuristic for the issue with the additional limitation. Van cave Berg presents a polynomial time calculation that takes care of the issue with the additional requirement to optimality. The creator likewise shows that the arrangement of the calculation for the issue with the additional requirement is all things considered 1.5 insurgencies of the merry go round over a lower headed for the issue without the additional limitation. He likewise uncovers that the upper bound of one upheaval introduced by Bartholdi and Platzman for their heuristic is wrong.

8.2. Relocation of storage:

Jaikumar and Solomon address the issue of re-finding beds with a high hope of recovery in an AS/RS to areas nearer to the I/O station during off-top hours. The creators expect that there is adequate time, so that movement time contemplations are excluded from the model. They present a productive calculation that limits the quantity of migrations to meet the normal throughput.

Muralidharan consolidate the advantages of randomized stockpiling (less extra room) and class-based capacity (less travel time). They recommend randomized area task while putting away beds and migration of beds regarding their turnover rates during inactive periods.

8.3. Dwell point positioning:

The dwell point in an AS/RS is the position where the S/R machine dwells when the framework is inactive. The abide point is chosen with the end goal that the normal travel time to the situation of the principal exchange after the inactive period is limited. A compelling stay point methodology might lessen the reaction seasons of the AS/RS, since the SIR machine regularly plays out a grouping of activities following an inactive period. Thus, assuming the primary activity is progressed, all tasks inside the arrangement are finished before.

The choice of the abide point has gotten impressive consideration in the writing. Graves select the stay point at the info/yield (I/O) station. Park shows the optimality of this procedure, if the likelihood of the main activity after an inactive period being a capacity is essentially 0.5. Egbelu presents LP-models for finding the stay point that limits the normal travel time and for finding the abide point that limits the greatest travel time to the primary exchange.

Egbelu and Wu use reproduction to assess the exhibition of a few abide point procedures. Hwang and Lim foster a technique that settles tracks down the ideal stay point as a Facility Location Problem with rectilinear distances. The computational intricacy of that strategy is comparable to arranging a bunch of numbers. All models that are referenced so far think about a discrete arrangement of capacity areas. Peters present an insightful model for tracking down the ideal stay point, in view of the articulations found by Bozer and White .

8.4. Dynamic control of warehouse:

Constant control of stockrooms is a mind boggling issue that arrangements with working conditions that change over the long run. To meet short-term throughput prerequisites of a fluctuating interest example, Jaikumar and Solomon (1990) look at the movement of beds which have a high anticipation of recovery in a future time-frame nearer to the P/D point. Expecting a specific distribution center setup and a twenty-class devoted capacity strategy, throughput increments by 15% (29%) when contrasted with when no movements are performed, considering that 10% (20%) of the every day load is moved.

9.conclusion:

Whether or not a warehousing issue is designated key, key or utilitarian, an ideal plan is reliably charming. Limit cutoff and stockroom design are indispensable decisions since they basically influence long stretch advantage. As these decisions don't rehash regularly, complex mathematical and amusement models are legitimized whether or not they are computationally expensive to handle.

For example, the task of items to capacity areas should mirror any adjustment of the item blend. Shared capacity approaches have been displayed to bring to the table superb potential for movement time and rack size decreases; consequently, further exploration on the subject appears to be beneficial. Obviously, the advantages of shared stockpiling should be weighed against the going with expansion in regulatory expense. The connection between various things is additionally a factor to be considered in building up a capacity strategy.

Functional choices incorporate picking and bunching arrangements, among others. Since these combinatorial issues will in general be settled more than once in down to earth circumstances, heuristics should be quick and yield great arrangements. Techniques for progressively further developing execution in stockroom tasks have as of late been presented.

Enormous incorporated models mirror the way that stockrooms are a part in more broad dissemination frameworks. Expenses considered incorporate the activity of offices, transportation of products among plants and dissemination focuses, inventories, and directing of conveyances to clients. Albeit some significant bits of knowledge can be acquired into the compromises between the various subsystems, one obstruction stays: that the subsystems them selves are coordinated authoritatively in discrete units, with the end goal that an ideal arrangement could demonstrate hard to execute.

We present survey on methods and techniques for the planning and control of warehousing systems. Planning refers to management decisions that affect the intermediate term (one or multiple months), such as inventory management and storage location assignment. Control refers to the operational decisions that affect the short term (hours, day), such as routing, sequencing, scheduling and order batching.

In This chapter we want to shows how to set up and solve a mixed-integer linear programming problem. The problem is to find the optimal production and distribution levels among a set of factories, warehouses, and sales outlets. For the problem-based approach.

The example first generates random locations for factories, warehouses, and sales outlets. Feel free to modify the scaling parameter N , which scales both the size of the grid in which the production and distribution facilities reside, but also scales the number of these facilities so that the density of facilities of each type per grid area is independent of N .

1. Facility Locations:

For a given value of the scaling parameter N , suppose that there are the following:

- $\lfloor fN^2 \rfloor$ factories
- $\lfloor wN^2 \rfloor$ warehouses
- $\lfloor sN^2 \rfloor$ sales outlets

These facilities are on separate integer grid points between 1 and N in the x and y directions. In order that the facilities have separate locations, you require that $f+w+s \leq 1$. In this example, take $N=20$, $f=0.05$, $w=0.05$, and $s=0.1$.

2. Production and Distribution:

There are P products made by the factories. Take $P=20$.

The demand for each product p in a sales outlet s is $d(s,p)$. The demand is the quantity that can be sold in a time interval. One constraint on the model is that the demand is met, meaning the system produces and distributes exactly the quantities in the demand.

- The are capacity constraints on each factory and each warehouse.
- The production of product p at factory f is less than $pcap(f,p)$.
- The capacity of warehouse w is $wcap(w)$.
- The amount of product p that can be transported from warehouse w to a sales outlet in the time interval is less than $turn(p)*wcap(w)$, where $turn(p)$ is the turnover rate of product p .

Suppose that each sales outlet receives its supplies from just one warehouse. Part of the problem is to determine the cheapest mapping of sales outlets to warehouses.

3. Costs:

The cost of transporting products from factory to warehouse, and from warehouse to sales outlet, depends on the distance between the facilities, and on the particular product. If $dist(a,b)$ is the distance between facilities a and b , then the cost of shipping a product p between these facilities is the distance times the transportation cost $tcost(p)$:

$$dist(a,b)*tcost(p).$$

The distance in this example is the grid distance, also known as the L_1 distance. It is the sum of the absolute difference in x coordinates and y coordinates.

The cost of making a unit of product p in factory f is $pcost(f,p)$.

3. Optimization Problem:

Given a set of facility locations, and the demands and capacity constraints, find:

- A production level of each product at each factory.

- A distribution schedule for products from factories to warehouses.
- A distribution schedule for products from warehouses to sales outlets.

These quantities must ensure that demand is satisfied and total cost is minimized. Also, each sales outlet is required to receive all its products from exactly one warehouse.

4. Variables and Equations for the Optimization Problem:

The control variables, meaning the ones you can change in the optimization, are

- $x(p,f,w)$ = the amount of product p that is transported from factory f to warehouse w .
- $y(s,w)$ = a binary variable taking value 1 when sales outlet s is associated with warehouse w .

The objective function to minimize is

$$\sum_f \sum_p \sum_w x(p, f, w) \cdot (pcost(f, p) + tcost(p) \cdot dist(f, w))$$

+

$$\sum_s \sum_w \sum_p (d(s, p) \cdot tcost(p) \cdot dist(s, w) \cdot y(s, w)).$$

The constraints are

$$\sum_w x(p, f, w) \leq pcap(f, p) \quad (\text{capacity of factory}).$$

$$\sum_f x(p, f, w) = \sum_s (d(s, p) \cdot y(s, w)) \quad (\text{demand is met}).$$

$$\sum_p \sum_s \frac{d(s, p)}{turn(p)} \cdot y(s, w) \leq wcap(w) \quad (\text{capacity of warehouse}).$$

$$\sum_w y(s, w) = 1 \quad (\text{each sales outlet associates to one warehouse}).$$

$$x(p, f, w) \geq 0 \quad (\text{nonnegative production}).$$

$$y(s, w) \in \{0, 1\} \quad (\text{binary } y).$$

The variables x and y appear in the objective and constraint functions linearly. Because y is restricted to integer values, the problem is a mixed-integer linear program (MILP).

Generate a Random Problem: Facility Locations:

Set the values of the N , f , w , and s parameters, and generate the facility locations.

```
rng(1) % for reproducibility
N = 25; % N from 10 to 30 seems to work. Choose large values with
caution.
N2 = N*N;
f = 0.05; % density of factories
w = 0.05; % density of warehouses
s = 0.1; % density of sales outlets
```

```
F = floor(f*N2); % number of factories
W = floor(w*N2); % number of warehouses
S = floor(s*N2); % number of sales outlets
```

```
xyloc = randperm(N2,F+W+S); % unique locations of facilities
[xloc,yloc] = ind2sub([N N],xyloc);
```

Of course, it is not realistic to take random locations for facilities. This example is intended to show solution techniques, not how to generate good facility locations.

Plot the facilities. Facilities 1 through F are factories, $F+1$ through $F+W$ are warehouses, and $F+W+1$ through $F+W+S$ are sales outlets.

```
h = figure;
plot(xloc(1:F),yloc(1:F),'rs',xloc(F+1:F+W),yloc(F+1:F+W),'k*',...
     xloc(F+W+1:F+W+S),yloc(F+W+1:F+W+S),'bo');
lgnd = legend('Factory','Warehouse','Sales
outlet','Location','EastOutside');
lgnd.AutoUpdate = 'off';
xlim([0 N+1]);ylim([0 N+1])
```

Generate Random Capacities, Costs, and Demands:

Generate random production costs, capacities, turnover rates, and demands.

```
P = 10; % 10 products

% Production costs between 20 and 100
pcost = 60*rand(F,P) + 20;

% Production capacity between 500 and 1500 for each product/factory
pcap = 600*rand(F,P) + 500;

% Warehouse capacity between P*400 and P*800 for each product/warehouse
wcap = P*500*rand(W,1) + P*500;

% Product turnover rate between 1 and 3 for each product
turn = 2*rand(1,P) + 1;

% Product transport cost per distance between 5 and 10 for each product
tcost = 5*rand(1,P) + 5;

% Product demand by sales outlet between 200 and 500 for each
% product/outlet
d = 300*rand(S,P) + 200;
```

These random demands and capacities can lead to infeasible problems. In other words, sometimes the demand exceeds the production and warehouse capacity constraints. If you alter some parameters and get an infeasible problem, during solution you will get an exitflag of -2.

Generate Variables and Constraints:

To begin specifying the problem, generate the distance arrays `distfw(i,j)` and `distsw(i,j)`.

```
distfw = zeros(F,W); % Allocate matrix for factory-warehouse distances
for ii = 1:F
    for jj = 1:W
```

```

        distfw(ii,jj) = abs(xloc(ii) - xloc(F + jj)) + abs(yloc(ii) ...
            - yloc(F + jj));
    end
end

```

```

distsw = zeros(S,W); % Allocate matrix for sales outlet-warehouse
distances
for ii = 1:S
    for jj = 1:W
        distsw(ii,jj) = abs(xloc(F + W + ii) - xloc(F + jj)) ...
            + abs(yloc(F + W + ii) - yloc(F + jj));
    end
end
end

```

Create variables for the optimization problem. x represents the production, a continuous variable, with dimension P -by- F -by- W . y represents the binary allocation of sales outlet to warehouse, an S -by- W variable.

```

x = optimvar('x',P,F,W,'LowerBound',0);
y = optimvar('y',S,W,'Type','integer','LowerBound',0,'UpperBound',1);

```

Now create the constraints. The first constraint is a capacity constraint on production.

```

capconstr = sum(x,3) <= pcap';

```

The next constraint is that the demand is met at each sales outlet.

```

demconstr = squeeze(sum(x,2)) == d'*y;

```

There is a capacity constraint at each warehouse.

```

warecap = sum(diag(1./turn)*(d'*y),1) <= wcap';

```

Finally, there is a requirement that each sales outlet connects to exactly one warehouse.

```

salesware = sum(y,2) == ones(S,1);

```

Create Problem and Objective:

Create an optimization problem.

```
factoryprob = optimproblem;
```

The objective function has three parts. The first part is the sum of the production costs.

```
objfun1 = sum(sum(sum(x,3).*(pcost'),2),1);
```

The second part is the sum of the transportation costs from factories to warehouses.

```
objfun2 = 0;
for p = 1:P
    objfun2 = objfun2 + tcost(p)*sum(sum(squeeze(x(p, :, :)).*distfw));
end
```

The third part is the sum of the transportation costs from warehouses to sales outlets.

```
r = sum(distsw.*y,2); % r is a length s vector
v = d*(tcost(:));
objfun3 = sum(v.*r);
```

The objective function to minimize is the sum of the three parts.

```
factoryprob.Objective = objfun1 + objfun2 + objfun3;
```

Include the constraints in the problem.

```
factoryprob.Constraints.capconstr = capconstr;
factoryprob.Constraints.demconstr = demconstr;
factoryprob.Constraints.warecap = warecap;
factoryprob.Constraints.salesware = salesware;
```

Solve the Problem:

Turn off iterative display so that you do not get hundreds of lines of output. Include a plot function to monitor the solution progress.

```
opts =  
optimoptions('intlinprog','Display','off','PlotFcn',@optimplotmilp);
```

Call the solver to find the solution.

```
[sol,fval,exitflag,output] = solve(factoryprob,'options',opts);  
  
if isempty(sol) % If the problem is infeasible or you stopped early with  
no solution  
    disp('The solver did not return a solution.')    return % Stop the script because there is nothing to examine  
end
```

Examine the Solution:

Examine the exit flag and the infeasibility of the solution.

```
exitflag  
infeas1 = max(max(infeasibility(capconstr,sol)))  
infeas2 = max(max(infeasibility(demconstr,sol)))  
infeas3 = max(infeasibility(warecap,sol))  
infeas4 = max(infeasibility(salesware,sol))
```

Round the yportion of the solution to be exactly integer-valued. To understand why these variables might not be exactly integers, see [Some "Integer" Solutions Are Not Integers](#).

```
sol.y = round(sol.y); % get integer solutions
```

How many sales outlets are associated with each warehouse? Notice that, in this case, some warehouses have 0 associated outlets, meaning the warehouses are not in use in the optimal solution.

```
outlets = sum(sol.y,1)
```

Plot the connection between each sales outlet and its warehouse.

```
figure(h);  
hold on
```

```
for ii = 1:S
    jj = find(sol.y(ii,:)); % Index of warehouse associated with ii
    xsales = xloc(F+W+ii); ysales = yloc(F+W+ii);
    xwarehouse = xloc(F+jj); ywarehouse = yloc(F+jj);
    if rand(1) < .5 % Draw y direction first half the time

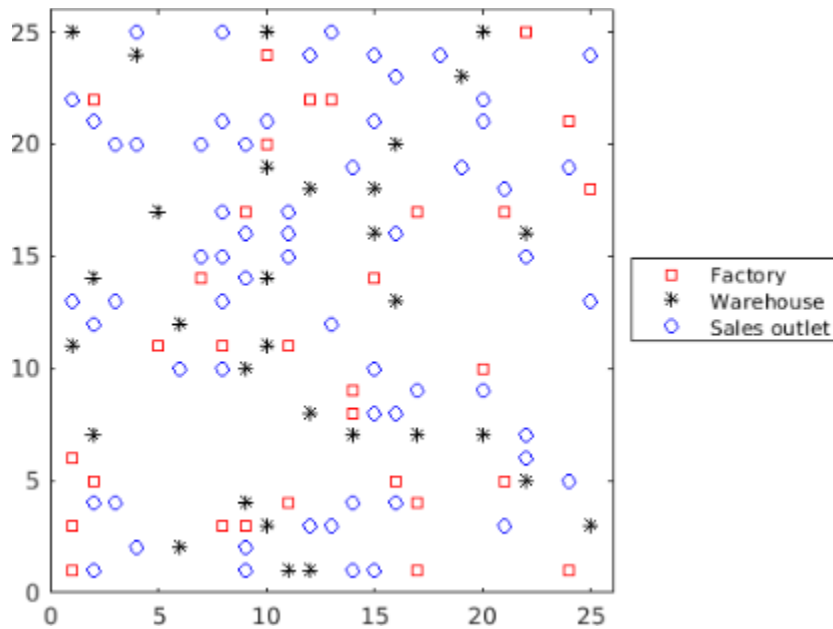
plot([xsales,xsales,xwarehouse],[ysales,ywarehouse,ywarehouse],'g--')
        else % Draw x direction first the rest of the time

plot([xsales,xwarehouse,xwarehouse],[ysales,ysales,ywarehouse],'g--')
    end
end
hold off
```

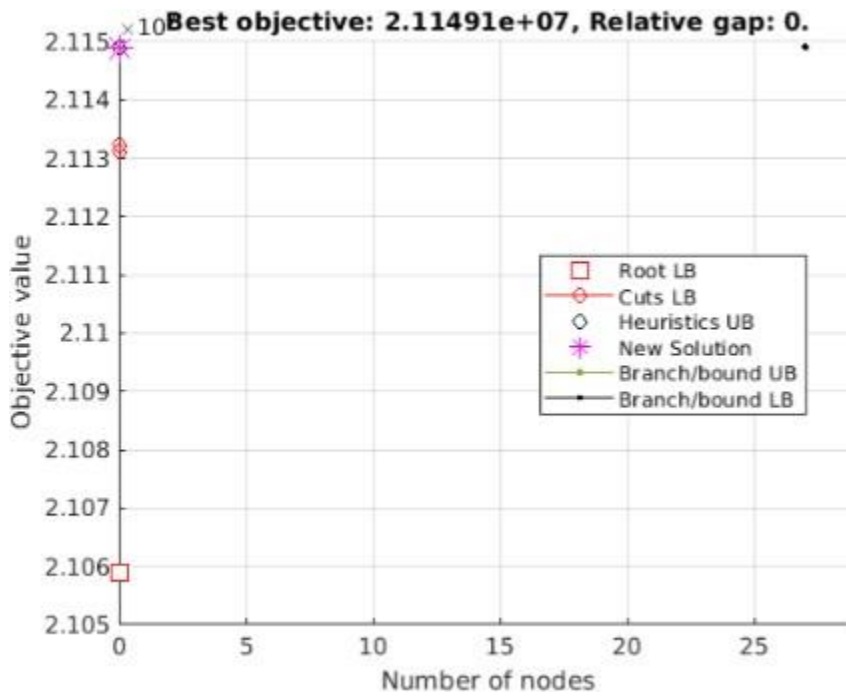
```
title('Mapping of sales outlets to warehouses')
```

The Result of program:

In the graph below we can see the generation of factories, warehouses, and sales outlets randomly.



So that we can decide what are the connections between the sales outlet and its warehouse, we have to determine the best objective in three parts (the sum of the production costs, the sum of the transportation costs from factories to warehouses, the sum of the transportation costs from warehouses to sales outlets.). So in the graph below we can see the value of best objective function to minimize is the sum of the three parts.



```

exitflag =
    OptimalSolution
infeas1 = 1.1369e-12
infeas2 = 1.0232e-12
infeas3 = 0
infeas4 = 3.3307e-15
    
```

To terminate our results by the connection, we can see in the graph below the better connection between each sales outlet and its warehouse.



Conclusion:

In This section we concluded the best way to set up and tackle a blended number direct programming issue. The issue is to track down the ideal creation and conveyance levels among a bunch of plants, distribution centers, and deals outlets. For the issue based methodology.

The model initially creates arbitrary areas for processing plants, distribution centers, and deals outlets. the scaling boundary N, which scales both the size of the network wherein the creation and dissemination offices live, yet in addition scales the quantity of these offices so the thickness of offices of each kind per framework region is autonomous of N.

Conclusions:

This paper has all the while thought about the item assignment and useful region size assurance issues in the plan of a stockroom. It gives a numerical model and a heuristic calculation to tackle the two issues mutually with the goal that yearly giving and capacity expenses can be limited. The info information necessity for this model is promptly accessible in many distribution centers and the model thinks about reasonable requirements. We accept this is the main accessible model that considers the two issues at the same time and permits the client to tackle them ideal Planning and control of warehousing frameworks are intricate issues. In this paper we have characterized a progressive system of warehousing choices, that will give great answers for these complicated issues. The overview shows that numerous techniques and strategies have been fostered that fundamentally beat the strategies that are utilized by and by. Indeed, even current data innovation, for example, specific distribution center administration frameworks actually utilize basic heuristics. Much of the time, the stockroom execution would be worked on by something like 10 shrewd arranging and control systems. In the wake of finishing the study, we might want to make two summing up comments. Right off the bat, hardly any papers have been distributed that current calculations which give ideal arrangements. Adjacent to their ideal presentation, these careful calculations give us understanding into the issues and they might be utilized as seat marks for heuristic systems. As the study shows, most papers talk about heuristic techniques. The utilization of heuristics is roused by the way that most warehousing issues are NP-hard in general. The commitment of such investigations might be significant if the heuristic gives a most pessimistic scenario bound or then again if a fascinating new model definition has been introduced. Thusly, we might want to pressure that more exertion ought to be given to the advancement of new models. Planning new models will set up bigger investment funds than streamlining the current ones. Unmistakably, presenting new working strategies will accomplish bigger investment funds than enhancing the current working systems.

seen that huge time investment funds are conceivable by permitting request picking from the save region. These reserve funds significantly surpassed the reserve funds between various allotment runs Secondly, numerous distributions in the overview examine strategies and models that endeavor to limit travel time in this way expanding throughput. Be that as it may, in most pragmatic circumstances amplifying throughput isn't the main target. Orders frequently need to fulfill time constraints so that compromises should be made among usefulness and criticalness.

Resume:

In a modern business, data must flow efficiently between production and warehouses, and between warehouses and sales outlets. These data represent in the first place: quantity, maturity, location. A better management of this data has only been achieved by a good optimization of its data. In this Master thesis we present an overview on the basics of this field, models, methods and we show how to configure and solve a linear programming problem with mixed integers. The problem is to find the optimal levels of production and distribution among a set of factories, warehouses and sales outlets.

Résumé:

Dans une entreprise moderne, les données doivent circuler efficacement entre la production et les entrepôts, et entre les entrepôts et les points de vente. Ces données représentent en premier lieu : la quantité, la maturité, la localisation. Une meilleure gestion de ces données n'a été obtenue que par une bonne optimisation de ses données. Dans ce mémoire, nous présentons un aperçu des bases de ce domaine, des modèles, des méthodes et nous montrons comment configurer et résoudre un problème de programmation linéaire avec des nombres entiers mixtes. Le problème est de trouver les niveaux optimaux de production et de distribution parmi un ensemble d'usines, d'entrepôts et de points de vente.

ملخص:

في الأعمال التجارية الحديثة، يجب أن تتدفق البيانات بكفاءة بين الإنتاج والمستودعات، وبين المستودعات ومنافذ البيع. تمثل هذه البيانات في المقام الأول: الكمية، والنضج، والموقع. تم تحقيق إدارة أفضل لهذه البيانات فقط من خلال التحسين الجيد لبياناتها. في أطروحة الماجستير هذه، نقدم نظرة عامة على أساسيات هذا المجال والنماذج والطرق ونعرض كيفية تكوين مشكلة البرمجة الخطية وحلها بأعداد صحيحة مختلطة. تكمن المشكلة في إيجاد المستويات المثلى للإنتاج والتوزيع بين مجموعة من المصانع والمستودعات ومنافذ البيع.

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